Structural Transformation, Education and Growth

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Introduction

General Question:

- Do all countries go through the same process of Structural Transformation (ST)?

    - **Many recent papers:** Common features across most countries.
        - Focus in preferences and technology.

    - **This paper:** A crucial difference between countries with different growth/development success.
        - Focus in policies on human capital.

Introduction

- **Common (& commonly studied) facts of ST:**
  - Initially: Shift of labor from aggriculture (A) to manufacturing (M) and services (S).
    - This initial process leads to increased aggregate productivity.
    - Long standing puzzle: why poor countries allocate labor to A.
  - At a later stage: shift from M to S;
    - decline in overall share of M.
    - S end up dominating total VA and labor.
    - Overall income and growth performance of country driven by S.

Introduction

- **Lesser known: Wide differences in skill-intensity in S.**

  - *Success growth stories: S in high skill sectors.*
    - *Services:* designers, researchers, chefs, social workers, inv. bankers.
    - Innovation/adoption/skills in S: drive countries to grow.
    - Examples: Developed countries (late); South Korea.

  - *Not so successful stories: S in low skill sectors.*
    - *Services:* street vendors, handymen, domestic labor, and moneylenders
    - Low skill accumulation/innovation S: ceiling for growth.
    - Examples: Brazil; other Latin American after 1980s.

Introduction

Policies?

- **Trade/industrial policies:**
  - Usual story when comparing South East Asia vs. Latin America
  - Perhaps, but:
    - **S** are mostly non-tradeables.
    - 1980s onward: *Convergence* of policies & *divergence* of incomes.

- **Human Capital Policies:**
  - New workers:
    - If unskilled: low (measured) productivity growth in S.
    - If skilled: high (measured) productivity growth in S.
  - Can also look at implications for demographic change.

This Paper:

A Simple *Quantitative* Model:

- **Education and Fertility:** Quantity/Quality of Children.
  - Parents choose number & skills of children (as in Becker).

- **Structural Transformation:**
  - *Sectors and Skills:*
    - *Agriculture:* low skills only.
    - *Manufacturing:* high skills only.
    - *Services:* low and high skills.
  - *Exogenous sectoral productivities.*
  - *Non-homothetic preferences.*

This Paper:

- **Education/Demographic Policies:**

  - *Two Policies:*
    - Child labor (allowed or not)
    - Schooling subsidies (funded with labor taxes).

  - *Redistribution with endogenous types.*

- **Calibration:**

  - *Two Countries: South Korea and Brazil, 1960-2005*
    - **Korea:** fast growth after 1980; Services: high producitivity/skills
    - **Brazil:** slow growth after 1980; Services: low producitivity/skills.

  - Model: education policies explain a big chunk of differences.

Related Literature

- **Structural transformation:**
  - Duarte and Restuccia (2010); Herrendorf, Rogerson and Valentinyi (2013), Ferreira and Silva (2014), McMillan and Rodrik (2011).
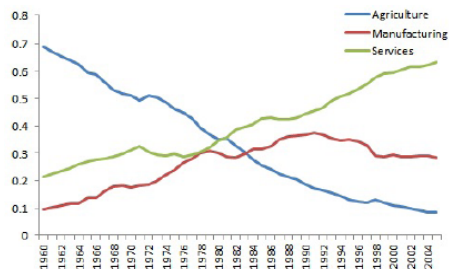 - *Souh Korea:* Betts, Giri and Verma (2013), Kim and Topel (1995).

- **Demographic Transition and Human Capital:**
  - Fertility and Education: Becker (1960), Becker, Murphy, and Tamura (1990), De la Croix and Doepke (2013), Doepke (2004).
  - *DGE models:* Erosa, Koreshkova and Restuccia (2010); Restuccia and Vandenbroucke (2013).
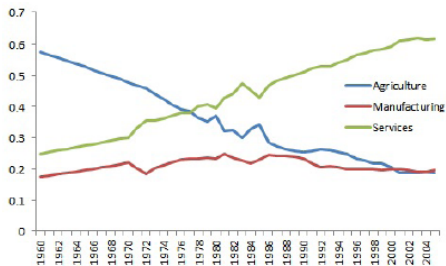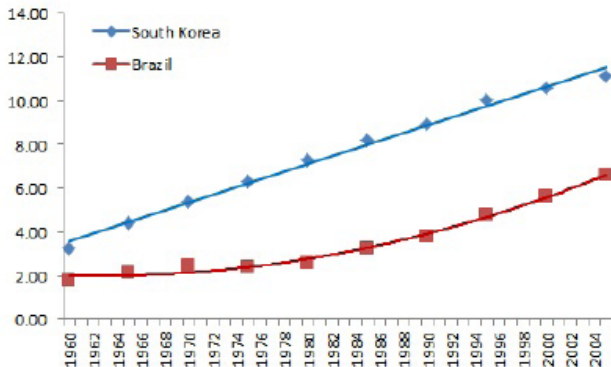
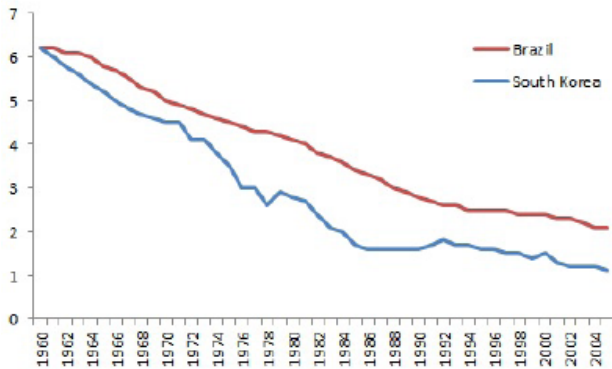Brazil: Allocation of Labor   Korea: Allocation of Labor

Sectoral allocation of Labor

Brazil and Korea: Education Trends Differences

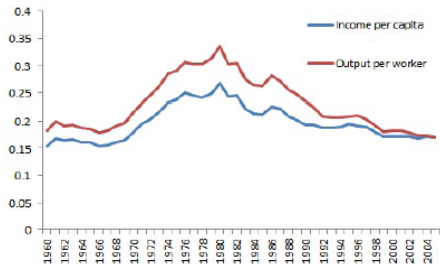Average years of schooling,
(economically active population)

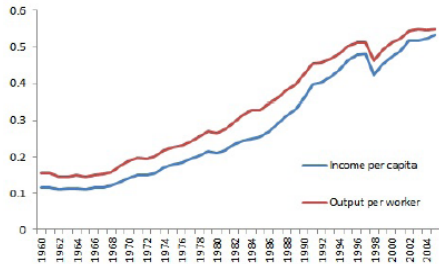# Brazil and Korea: Fertility Differences

Total Fertility Rates

(a) Brazil

(b) South Korea

Output per worker and per person.

The Model

- *Demographics:*
  - Two period lived OLG; $t = 0, 1, 2....$
  - Lifetime decisions:
    - 1st period: children: work or not; attend school or not.
    - 2nd period: adults: labor market; number and skill of children.

- *Preferences:*
  - Altruistic Parents: current utility and utility of offspring.
  - Non-homothetic preferences wrt to three goods:

- *Production Sectors and Skills:*
  - *Agriculture:* low skills only.
  - *Manufacturing:* high skills only.
  - *Services:* low and high skills.

- *Exogenous sectoral productivities.*

- *Exogenously given policies.*

The Model

- **Demographics:** Adult types:
    1. **Skilled (H)**, if they went to school.
    2. **Unskilled (L)**, if they didn't.
        - Child labor $\implies$ No school.

    - N_H: number of skilled adults.
    - N_L: number of unskilled adults.

- *Production Sectors and Skills:*
    - *Agriculture:* low skills only $\qquad Y_A = Z_A L_{AL}.$
    - *Manufacturing:* high skills only $\qquad Y_M = Z_M L_{MH}..$
    - *Services:* low and high skills $\qquad Y_S = Z_S (L_{SH})^\alpha (L_{SL})^{1-\alpha}.$

- *Exogenous sectoral productivities:* $\qquad Z'_j = (1 + \gamma_j) Z_j.$

- **State of the Economy:** $\qquad X \equiv \{Z_A, Z_M, Z_S, N_H, N_L\}.$

The Model

- **Production:** All sectors $j = A, M, S$, are perfectly competitive:

$$\max_{l_{jH}, l_{jL}} \; p_j(X) \, Y_j(l_{jH}, l_{jL}) - w_H(X) l_{jH} - w_L(X) l_{jL},$$

- Free entry + FOC:

$$w_L(X) = p_A(X) Z_A = p_S(X) Z_S (1 - \alpha) \left[\frac{L_{SH}(X)}{L_{SL}(X)} \right]^{\alpha}$$

$$w_H(X) = p_M(X) Z_M = p_S(X) Z_S \alpha \left[\frac{L_{SL}(X)}{L_{SH}(X)} \right]^{1-\alpha}$$

- and $L_{AH} = L_{ML} = 0$.

The Model

Households:

- **Preferences:** An adult's utility:

$$V(u, n_H, n_L) = U + \beta(n_H + n_L)^{-\varepsilon}[n_H V_H^{'} + n_L V_L^{'}],$$

where

$$U(c_A, c_M, c_S) = \frac{\left[v(c_A)(c_M)^b(c_S + \bar{c}_S)^{(1-b)}\right]^{1-\sigma}}{1 - \sigma},$$

$$v(c_A) = \begin{cases} 0 & \text{if} \quad c_A < \bar{c}_A \\ 1 & \text{if} \quad c_A \geq \bar{c}_A \end{cases}.$$

here $\varepsilon > 0$ and $\sigma, b \in (0, 1)$.

- **Time Allocation:** Work and raising children.
  - Raising a child: each child takes a fraction $\phi > 0$ of time.
    - If skilled child: addtional $\phi_H > 0$ of units of skilled (teacher's) time.
    - If unskilled: if allowed to work, $0 \leq \phi_L < \phi$ units of unskilled labor.

The Model

- **Government Policies:** Schooling subsidies & child labor restrictions.

  - **Education subsidies:** The government subsidizes a fraction δ of the educational costs.
    - Financing: proportional income tax $\tau(X)$, s.t. budget balance.
    - $(\delta, \tau(X))$ is a regressive tax program (taxes paid even if unskilled).

  - **Child labor policies:** Limit on the number of hours a child can work.
    - Equivalent to reductions on returns of child labor to ϕ_L^g: $0 \leq \phi_L^g < \phi_L$.

Equilibrium

Definition

Let $j \in \{A, M, S\}$ index the sectors and $i, k \in \{L, H\}$ index the skill/school levels of the population. Given an initial state $X_0 \in \mathbb{R}^5_+$, exogenous growth rates $\{\gamma_A, \gamma_M, \gamma_S\}$ and government policies $\{\delta, \phi_L^g\}$, an **equilibrium** in this economy is: *(a)* a low of motion $\Lambda : \mathbb{R}^5_+ \rightarrow \mathbb{R}^5_+$, for the state X; *(b)* price and wage functions $p_j : \mathbb{R}^5_+ \rightarrow \mathbb{R}_+$, and $w_i : \mathbb{R}^5_+ \rightarrow \mathbb{R}_+$, *(c)* labor allocations $L_{j,i} : \mathbb{R}^5_+ \rightarrow \mathbb{R}_+$, and consumption and fertility decisions, $c_{i,j} : \mathbb{R}^5_+ \rightarrow \mathbb{R}_+$ and $n_{i,k} : \mathbb{R}^5_+ \rightarrow \mathbb{R}_+$; and *(d)* a tax function $\tau : \mathbb{R}^5_+ \rightarrow [0, 1]$, such that: **(i)** for any X in the current period, the state X' in the next period is given by $X' = \Lambda(X)$; **(ii)** given prices $\{w_i(\cdot), p_j(\cdot)\}$, (1) the allocations $\{L_{j,i}(\cdot)\}$ solve the firms problem; (2) the allocations $\{c_{i,j}(\cdot), n_{i,k}(\cdot)\}$ solve the household problem; (3) the goods and labor markets clear; (4) the budget constraint of the government balances (i.e. the tax rate is given by (1); and **(iii)** the transition $\Lambda(\cdot)$ is given by the growth rates by $\{\gamma_A, \gamma_M, \gamma_S\}$ and the fertility and education decisions $\{n_{i,k}(\cdot)\}$.

Equilibrium

An adult of type $i \in \{H, L\}$:

$$V_i(X) = \max_{c_A, c_M, c_S, n_L, n_H \geq 0} \left\{ U + \beta(n_H + n_L)^{-\varepsilon}[n_H V_H' + n_L V_L'] \right\},$$

subject to:

$$\sum_{j \in \{A, M, S\}} p_j c_j + (1 - \delta)\phi_H w_H(X) n_H$$

$$\leq (1 - \tau(X)) \left\{ w_i(X) \left[1 - \phi(n_H + n_L) \right] + \phi_L^g w_L(X) n_L \right\}.$$

For each adult, the values V_H' and V_L' given by the law of motion of X'.

Equilibrium

- Let $n_{i,j}(X)$: number of children of type j that parents of type i have.

- **Population law of motion:**

$$\left[\begin{array}{c} N'_H \\ N'_L \end{array} \right] = \left[\begin{array}{cc} n_{H,H}(X) & n_{L,H}(X) \\ n_{H,L}(X) & n_{L,L}(X) \end{array} \right] \left[\begin{array}{c} N_H \\ N_L \end{array} \right].$$

Equilibrium

- **Total supply of skilled labor**:

$$L_H(X) = \left[1 - (\phi + \phi_H)n_{H,H}(X) - \phi n_{H,L}(X)\right] N_H - \phi_H n_{L,H}(X) N_L.$$

- **Total supply of unskilled labor:**

$$L_L(X) = \left[1 - \phi n_{L,H}(X) - \phi n_{L,L}(X)\right] N_L + \phi_L^g \left[n_{H,L}(X)N_H + n_{L,L}(X)N_L\right].$$

Equilibrium

- **Market-clearing labor markets:**
  - Skill workers: option to be unskilled:

  $$w_H(X) \geq w_L(X).$$

  - Unskilled labor market clearing:

  $$L_{MH}(X) + L_{SH}(X) \leq L_H(X) \qquad (\text{with} = \text{if } w_H(X) > w_L(X)),$$

  - Skilled labor market clearing:

  $$L_{AL}(X) + L_{SL}(X) = L_L(X) + [L_H(X) - L_{MH}(X) - L_{SH}(X)].$$

Equilibrium

- **Market-clearing labor markets:** As long as $L_L > \frac{\bar{c}_A}{Z_A}(N_L + N_H)$, unique $L_{H,M}$:

$$\left[1 + \frac{\alpha(1-b)}{b}\right] L_{H,M} = L_H + \frac{\bar{c}_S(N_L + N_H)\left[L_H - L_{H,M}\right]^{1-\alpha}}{Z_S\left[L_L - \frac{\bar{c}_A}{Z_A}(N_L + N_H)\right]^{1-\alpha}}.$$

and all $\left\{w_i(X), p_j(X)\right\}$ can be solved.

- **Budget Constraint of the Government:** Balanced every period:

$$\tau(X) = \frac{\delta\phi_H N_H'(X)}{L_H(X) + \phi_H N_H' + L_L(X)\frac{w_L(X)}{w_H(X)}}, \tag{1}$$

Some Simple Analytics

- Let the costs of each type of child for parents $i = L, H$:

  - Skilled child:
    $$p_H^i = \phi w_i + \phi_H (1 - \delta) w_H;$$

  - Unskilled child:
    $$p_L^i = \phi w_i - \phi_L^g w_L.$$

- An alternative way of formulating the problem: Adults chose

  - The total expenditure E on child rearing ($E = p_H + p_L$);

  - The fraction f that will be spent with skilled children

Some Simple Analytics

- **The intratemporal problem:** Given any w and E:

$$\bar{U}\left(w - E\right) = \max_{c_j} U\left(c\right),$$

$$\text{s.t.:} \qquad \sum_{j \in \{A,M,S\}} p_j c_j \leq w - E.$$

- **The intertemporal problem:** Given w, choose $E \leq w$, $f \in [0, 1]$:

$$V_i = \max_{E, f} \left\{ \bar{U}\left(w_i - E\right) + \beta E^{1-\varepsilon} \left(\frac{f}{p_H^i} + \frac{(1-f)}{p_L^i} \right) \left[\frac{fV_H'}{p_H^i} + \frac{(1-f)V_L'}{p_L^i} \right] \right\}$$

Some Simple Analytics

- Assumed preferences: high-low skilled children are perfect substitutes.
  - indifference curves (n_H, n_L) are straight lines.

Proposition

For all $\{E, f\}$, that attains the maximum in (1), the solution is $f = 0$ or $f = 1$, i.e., the problem of adult has only corner solutions. So adults of each type choose only to have one type of child, that is, there are never both skilled and unskilled children within the same family.

- Only corner solutions: $f_i = 0$ or $f_i = 1$.
  - $n_{i,H}, n_{i,L}$ by comparing solutions with only one type of child.

Some Simple Analytics

Proposition

An adult is indifferent between both types of children if, and only if the costs and utilities of children satisfy the following condition:

$$\frac{V_S}{p_S^{1-\varepsilon}} = \frac{V_U}{p_U^{1-\varepsilon}} \tag{2}$$

If an adult is indifferent, the total expenditure on children does not depend on the type of child chosen.

Some Simple Analytics

- If $w_H > w_L$: skilled children relatively cheaper for skilled parents:

$$\frac{\phi w_H + \phi_H \left(1 - \delta\right) w_H}{\phi w_H - \phi_L^g w_L} < \frac{\phi w_L + \phi_H \left(1 - \delta\right) w_H}{\phi w_L - \phi_L^g w_L}.$$

- Parents of different skills cannot simulateneously be indifferent between the two types of children.

- In our calibration: equilibrium with intergenerational upward mobility.
    - High-skilled parents: only high-skilled children.
    - Low-skilled parents: indifferent between the two types of children.

- **Partial equilibrium:** Given $\left\{ w_i^t,\ p_j^t,\ \tau^t \right\}_{t=0}^{\infty}$.

  - Relaxing child labor: higher ϕ_L^g:
    - Higher V_L, higher $n_{L,L}$, partly due to higher V_L'.

  - Higher subsidies to eduction: higher δ:
    - Higher V_H, higher $n_{H,H}$, partly due to higher V_H'.

Impact of Policies

- **Redistributive:** Given $\left\{ w_i^t, \, p_j^t \right\}_{t=0}^{\infty}$, but τ *balancing GBC:*

  - Relaxing child labor: higher ϕ_L^g:
    - Higher V_L, higher $n_{L,L}$, partly due to higher V_L' and lower τ.
    - Higher V_H, higher $n_{H,H}$, partly due to and lower τ.

  - Higher subsidies to eduction: higher δ:
    - Higher V_H, higher $n_{H,H}$, despite higher τ.
    - Lower V_L, lower $n_{L,L}$, because higher τ (and hence lower V_L').

Calibration

- **Preferences:**.

Parameter	Value	Target/Source
β	0.132	Doepke (2004)
σ	0.5	"
ε	0.5	"
b	0.15	Herrendorf et al. (2011)
$\bar{c}_A$	by country/year	share labor in agriculture
$\bar{c}_S$	by country/year	match $C_S = Y_S$

Calibration

- **Technology, Production, Education:**

Parameter	Value		Target/Source
	Korea	**Brazil**	
α	0.40		PNAD
ϕ	0.155		Doepke(2004)
ϕ_H	0.04		"
δ	0.5	0.0	"
$\phi_{L,60-82}^g$	0.07	0.069	"
$\phi_{L,83-05}^g$	0	0.069	"

- *Sectoral productivity paths:* set as in Duarte and Restuccia (2010).
- Skilled labor *defined* as *"some secondary education"* (otherwise too few in 1960).

Results

- Growth rates:

  - *Calibrated model:* large gaps in the Korea vs. Brazil growth rates.

Growth: Output per worker	Brazil	Korea
PWT: $\frac{avg.\ 83-05}{avg.\ 60-82}$	18%	210%
Model:	36%	232%

Results: Allocation of workers across sectors

- **Initial:** 1960-1982; **Final:** 1983-2005

Variable	Brazil				Korea			
	Initial		Final		Initial		Final	
	Data	Model	Data	Model	Data	Model	Data	Model
N_H	0.10	0.31	0.27	0.35	0.29	0.49	0.70	0.74
L_{AL}/L_L	0.64	0.63	0.35	0.36	0.65	0.65	0.27	0.28
L_{MH}/L_H	0.74	0.77	0.67	0.67	0.81	0.82	0.74	0.69
L_{SL}/L_L	0.36	0.37	0.65	0.64	0.35	0.35	0.73	0.72
L_{SH}/L_H	0.26	0.23	0.33	0.34	0.19	0.18	0.26	0.31

- Overall: model matches share of skilled labor in Korea and Brazil for both periods.
  - Overestimates skilled workers (b.c.only skilled labor in M)

Total Fertility rate	Brazil		Korea	
	Data	Model	Data	Model
1982	3.8	2.3	2.4	2.2
2005	2.1	2.1	1.1	1.2

- Model close to the data in Korea.
  - Underestimates initial fertility in Brazil.

Counterfactuals: Education Policies and Growth

Brazil		**Korea**	
	Growth		Growth
Benchmark	36%	Benchmark	232%
Brazil: Korean policies	57%	Korea: Brazilian policies	112%

- Korea with Brazilian policies: **growth less than half.**
- Brazil with Korean polices: **growth 60% more.**

Counterfactual Policies: Fertility & Labor Allocation

Variable	Brazil				Korea			
	Benchmark		Korean Policies		Benchmark		Brazilian Policies	
	Initial	Final	Initial	Final	Initial	Final	Initial	Final
TFR	2.3	2.1	2.5	1.2	2.2	1.2	2.1	1.9
N_H	0.31	0.35	0.38	0.60	0.49	0.74	0.37	0.42
L_{AL}/L_L	0.63	0.36	0.73	0.57	0.65	0.28	0.62	0.13
L_{MH}/L_H	0.77	0.67	0.80	0.65	0.82	0.69	0.81	0.66
L_{SL}/L_L	0.37	0.64	0.27	0.43	0.35	0.72	0.38	0.87
L_{SH}/L_H	0.23	0.34	0.20	0.35	0.18	0.31	0.19	0.34

- **Brazil with Korean policies:**
  - Fertility rate first increases and then decreases.
  - Large increase (70%) in skilled workers in second period.

- **Korea with Brazilian policies:**
  - Fertility rate would remain high (1.9 instead of 1.2).
  - Skilled workers would decreases by almost 50%.

Concluding Remarks

- We incorporate fertility and education decisions to a structural transformation model.

- Calibrated the model to Korea and Brazil.
  - Model matches growth paths, fertility and labor allocation across skills and sectors.

- We use the model to understand impact of education policies.
  - Model helps explain the differences between Korea and Brazil.
  - Education subsidies and restrictions on child labor: help explain Koreans growth, human capital accumulation and structural transformation.

- Extension: Three skill levels, $i \in \{U, L, H\}$ and truly high skill services.