

Time-Series Estimation of Structural Import Demand Equations: A Cross-Country Analysis

ABDELHAK SENHADJI*

A structural import demand equation is derived and estimated for a large number of countries, using recent time-series techniques that address the problem of nonstationarity. The average price elasticity is close to zero in the short run but is slightly higher than one in the long run. A similar pattern holds for income elasticities: the short-run income elasticities are on average less than 0.5, while the long-run income elasticities are close to 1.5. The paper also analyses the small-sample properties of both the ordinary-least-squares (OLS) and the fully modified (FM) estimators of the short- and long-run elasticities, using Monte Carlo methods. [JEL F14, F41, E21, C22]

THE EMPIRICAL investigation of the import demand function has been one of the most active research areas in international economics. This is evidenced by the many surveys on this topic, although most focus on industrial countries.¹ Perhaps one of the main reasons for its popularity is its application to a wide range of important macroeconomic policy issues such as the impact of expenditure-switching through exchange rate management and commercial policy on a country's trade balance; the international trans-

*Abdelhak Senhadji is an Economist in the IMF Institute. He holds an M.A. in Econometrics from the University of Brussels and a Ph.D. in Economics from the University of Pennsylvania. He is grateful to participants in the Summer Econometric Society Meetings (June 21–24, 1996) and in the Midwest Macroeconomic Conference at Ohio State University (September 13–15, 1996), colleagues at the IMF Institute, and the referees for helpful comments. He is particularly indebted to Mohsin Khan and Masao Ogaki for insightful discussions. Patricia Laverley and Véronique Catany provided excellent editorial assistance.

¹ See Goldstein and Khan (1985) for a recent survey, and Faini, Pritchett, and Clavijo (1992) for an analysis of developing countries' imports.

mission of domestic disturbances, where these elasticities are a crucial link between economies; and the degree to which the external balance constraint affects a country's growth.

The traditional import demand function is specified as a log-linear function of the relative price of imports and real income. Because of data constraints and the empirical success of this specification, it has dominated the empirical literature for more than a quarter-century. But questions about its microeconomic foundation arise since it has not been derived from utility maximization. Another issue that has been largely ignored in the literature is the problem of nonstationarity, which is found in most macroeconomic variables and which invalidates classical statistical inference. Thus, if the variables that enter the import demand equation contain a unit root, ignoring nonstationarity in these variables may cause serious inference problems.

Empirical researchers are generally interested in two statistical properties of their estimates of import elasticities. First, they are interested in the magnitude of these elasticities. A relevant question, then, is how close the estimates are to their true value in small samples. The systematic deviation of the estimates from their true value is measured by the bias of the estimates. Second, they are interested in inference, that is hypotheses testing, about these estimates. For example, are the price and income elasticities significantly different from one? Testing such hypotheses requires knowing the distribution of the t -statistic (defined as the coefficient estimate divided by its standard deviation). The asymptotic distribution of this statistic is unknown for the long-run elasticities as these elasticities are nonlinear transformations of the import demand coefficients. In addition, the definition of the long-run elasticities includes the lagged dependent variable whose t -statistic follows a nonstandard distribution in the nonstationary case. In light of this, using the critical values of the asymptotic t -distribution for hypothesis testing may be misleading.

The objective of this paper is twofold. First, the paper seeks to address the two problems discussed above by deriving an empirically tractable import demand equation that can be estimated for a large number of countries, using recent time-series techniques that address the issue of nonstationarity present in the data. Second, the paper computes the exact bias as well as the exact distribution of the t -statistic, which is crucial for inference as discussed above, for the short- and long-run elasticities.

The derived aggregate import demand equation is log-linear in the relative price of imports and an activity variable defined as GDP minus exports.² An important insight from the explicit derivation of the aggregate

²As will be shown in Section I, the correct activity variable is GDP minus exports, not GDP as in the standard import demand equation.

import demand equation is that the definition of the activity variable depends on the aggregation level.³ The model predicts a unique cointegrating vector among imports, the relative price of imports, and the activity variable. This prediction is not rejected by the data, and the cointegrating vector is estimated both by ordinary least squares (OLS) and by the Phillips-Hansen fully modified (FM) estimator. Two recent papers follow a similar methodology. Clarida (1994) derives a similar import demand function for U.S. nondurable consumption goods from explicit intertemporal optimization, carefully taking into account data nonstationarity. Similarly, Reinhart (1995) estimates both structural import and export demand functions for 12 developing countries using Johansen's cointegration approach.

The results underscore the presence of nonstationarity in the data and the adverse consequences of neglecting it. Both price and income elasticities generally have the expected sign and are precisely estimated. The average price elasticity is close to zero in the short run but is slightly higher than one in the long run. It takes five years for the average price elasticity to achieve 90 percent of its long-run level. A similar pattern holds for income elasticities in the sense that imports react relatively slowly to changes in domestic income. The short-run income elasticities are on average less than 0.5, while the long-run income elasticities are close to 1.5. Industrial countries have both higher income and lower price elasticities than do developing countries. On average, these estimates are relatively close to Reinhart's.⁴

The analysis shows that the OLS bias is significantly higher than the FM bias for both the short- and long-run elasticity estimates. The FM bias reaches its minimum when the relative price of imports and the activity variable are exogenous. Strong endogeneity of the explanatory variables (that is, high correlation between the import demand innovations and the explanatory variables innovations) may induce substantial bias. But for most countries—being “small” relative to the rest of the world—the relative price of imports and the activity variable are only weakly endogenous, leading to a relatively small bias. For the benchmark case in which both explanatory variables are assumed to be exogenous, the *t*-statistics of the short-run elasticities are symmetric around zero but are flatter than the asymptotic *t*-distribution. This implies that inference based on the usual *t*- or *F*-statistic may be misleading. For example, the exact confidence inter-

³Because disaggregated import prices are not available for most developing countries, only aggregate import demand equations can be estimated. For highly disaggregated import demand equations for the United States, see Marston (1990) and Swagel (1995).

⁴Her average long-run price and income elasticities are -0.66 and 1.31 , respectively. The corresponding estimates in this paper are -1.08 and 1.45 . The small discrepancy may simply reflect different samples (these averages are over 12 countries in Reinhart and over 66 countries in this paper) as well as different estimation methods.

vals are significantly wider than those based on the asymptotic t -distribution. The distribution of the t -statistic for the short-run elasticities becomes skewed and flatter when the relative price of imports and/or the activity variable is allowed to be endogenous. The stronger the endogeneity, the larger is this departure from the asymptotic t -distribution.

I. The Model

Assume that the import decision in each country is made by an infinitely lived representative agent who decides how much to consume from the domestic endowment (d_t) and from the imported good (m_t).⁵ The home good is the numeraire. The intertemporal decision can be formalized by the following problem:

$$\begin{aligned} \text{Max} \quad & E_0 \sum_{t=0}^{\infty} (1 + \delta)^{-t} u(d_t, m_t) \\ & \{d_t, m_t\}_{t=0}^{\infty} \end{aligned} \quad (1)$$

subject to:

$$b_{t+1} = (1 + r)b_t + (e_t - d_t) - p_t m_t \quad (2)$$

$$e_t = (1 - \rho)\bar{e} + \rho e_{t-1} + \xi_t, \quad \xi_t \sim (0, \sigma^2) \quad (3)$$

$$\lim_{T \rightarrow \infty} \frac{b_{T+1}}{\prod_{t=0}^T (1 + r)^{-t}} = 0, \quad (4)$$

where δ is the consumer's subjective discount rate; r is the world interest rate; b_{t+1} is the next period stock of foreign bonds if positive, and the next period's debt level if negative; e_t is the stochastic endowment, which follows an AR(1) process with unconditional mean \bar{e} and an unconditional variance $\sigma^2/(1 - \rho^2)$, where σ^2 is the variance of the i.i.d. innovation ξ_t , and ρ determines the degree of persistence of the endowment shocks; and p_t is the relative price of the foreign good, that is, the inverse of the usual definition of terms of trade. In this two-good economy, p_t is also the real exchange rate. Equation (2) is the current account equation, equation (3) is

⁵The strong assumptions are necessary in order to derive an aggregate import demand equation that does not require more data than what is available. In particular, there is no production sector that implies that the model does not distinguish between intermediate and final goods.

the stochastic process driving the endowment shock, and equation (4) is the transversality condition that rules out Ponzi games. The first-order conditions of this problem are

$$u_t^d = \lambda_t \quad (5)$$

$$u_t^m = \lambda_t p_t \quad (6)$$

$$\lambda_t = (1 + \delta)^{-1} (1 + r) E_t \lambda_{t+1}, \quad (7)$$

where λ_t is the Lagrange multiplier on the current account equation. From equation (5), λ_t is the marginal utility of the domestic good. Following Clarida (1994) and Ogaki (1992), it is assumed that the instantaneous utility function u is addilog:⁶

$$u(d_t, m_t) = A_t d_t^{1-\alpha} (1-\alpha)^{-1} + B_t m_t^{1-\beta} (1-\beta)^{-1} \quad \alpha > 0, \beta > 0 \quad (8)$$

$$A_t = e^{a_0 + \varepsilon_{A,t}} \quad (9)$$

$$B_t = e^{b_0 + \varepsilon_{B,t}} \quad (10)$$

where A_t and B_t are exponential stationary random shocks to preferences, $\varepsilon_{A,t}$ and $\varepsilon_{B,t}$ are stationary shocks and α and β are curvature parameters. Substituting equation (8) into equations (5) and (6) yields

$$d_t = \lambda_t^{-\frac{1}{\alpha}} A_t^{\frac{1}{\alpha}} \quad (11)$$

$$m_t = \lambda_t^{-\frac{1}{\beta}} B_t^{\frac{1}{\beta}} p_t^{-\frac{1}{\beta}}. \quad (12)$$

Substituting equations (9)-(11) into equation (12) and taking logs yields

$$\tilde{m}_t = c - \frac{1}{\beta} \tilde{p}_t + \frac{\alpha}{\beta} \tilde{d}_t + \varepsilon_t, \quad (13)$$

where $c_0 = (1/\beta)(b_0 - a_0)$, and $\varepsilon_t = (1/b)(\varepsilon_{B,t} - \varepsilon_{A,t})$. A tilde indicates the log of the corresponding variable. In this model, $x_t = e_t - d_t = GDP_t - d_t$, where x_t is exports. Consequently, $d_t = GDP_t - x_t$. Thus, the model yields an equation for import demand that is close to the standard import demand function

⁶For the properties of the addilog utility function, see Houthakker (1960).

except that the correct activity variable is $GDP_t - x_t$, rather than GDP_t . Equation (13) can be rewritten as

$$\tilde{m}_t = c - \frac{1}{\beta} \tilde{p}_t + \frac{\alpha}{\beta} (\widetilde{GDP_t - x_t}) + \varepsilon_t. \quad (14)$$

Because each of the three variables in the import demand equation (14) can either be trend stationary (TS) or difference stationary (DS), four cases need to be considered (Table 1). In Section II, results from unit root tests show that the first case is the most common one, with some countries falling into the second category. The prime interest is the estimates of the standard price and income elasticities of the import demand ($-1/\beta$ and α/β , respectively). Note that \tilde{m}_t and \tilde{p}_t are, in general, endogenously determined by import demand and import supply (not modeled here). Therefore, \tilde{p}_t is likely to be correlated with the error term ε_t in equation (14). Thus, OLS would yield biased estimates of the price and income elasticities. As shown in the Appendix, the Phillips-Hansen FM estimator corrects within a cointegration framework, for this potential simultaneity bias as well as for autocorrelation in ε_t .

Equation (14) will be estimated in a dynamic form (that is, with the lagged dependent variable included as an explanatory variable) which proved to be more successful in the estimation stage, and also to keep the specification as close as possible to the literature where this autoregressive distributed lag (ARDL) specification has been widely used:⁷

$$\tilde{m}_t = \gamma_0 + \gamma_1 m_{t-1} + \gamma_2 \tilde{p}_t + \gamma_3 (\widetilde{GDP_t - x_t}) + \varepsilon_t. \quad (15)$$

While the lagged dependent variable enriches the dynamics of the import demand equation, its introduction into the cointegration framework outlined above is not innocuous as equation (15) resembles the error correction form of equation (14) except that the dependent variable and the two explanatory variables are in levels and not in first difference. Pesaran and Shin (1997) show that this ARDL specification is well specified and retains the usual interpretation under stationarity even if the variables are I(1). The authors also show that the FM estimator yields efficient estimates of the short- and long-run elasticities.

⁷A specification analysis by Thursby and Thursby (1984) shows that this type of dynamic specification outperforms the static ones. The lagged dependent variable can be introduced in the model by assuming some type of adjustment costs, see Goldstein and Khan (1985).

Table 1. *The Four Possible Model Specifications*

Model Specification	Model Predictions and Testing Strategy
<p>1. All three variables are difference stationary (DS)</p> <p>In the model, the following three assumptions are necessary to achieve DS for all three variables:</p> <p>a. For \tilde{d}_t to be DS, we must assume $r = \delta$. Then the Euler equation (7) becomes:</p> $\lambda_t = E_t \lambda_{t+1}$ <p>Thus, λ_t can be written as: $\lambda_t = \lambda_{t+1} + e_t$, where e_t is such that $E_t e_t = 0$. In other words, λ_t has a unit root and, therefore, \tilde{d}_t will also inherit a unit root since \tilde{A}_t is stationary. If d_t has a unit root, then, from equation (13), \tilde{m}_t will also have a unit root.</p>	<p>Under assumptions (a) – (c), equation (13) implies that \tilde{m}_t, \tilde{d}_t, and \tilde{p}_t are cointegrated with cointegrating vector $(1 \ 1/\beta - \alpha/\beta)$. Furthermore, this cointegrating vector is unique (up to a scale factor), since the import demand equation (13) has three I(1) variables and two common stochastic trends.^b If a cointegration relation between these three variables does not exist, estimation of the import demand equation (13) will result in a spurious regression. Hence, to detect this potential spuriousness, a residual-based cointegration test will be performed on equation (13).</p>
<p>b. The log of the relative price of imports will be assumed to be difference-stationary (we will see that this assumption cannot be rejected statistically for most countries).^a</p>	
<p>c. \tilde{p}_t and \tilde{d}_t are not cointegrated with cointegrating vector $(1 - \alpha)$.</p>	
<p>2. One of the three variables is trend stationary (TS)</p>	

We have three cases, depending on which variable is TS

<p>a. \tilde{m}_t is TS.</p> <p>The model would yield this case under the following three assumptions: \tilde{p}_t is DS; assumption (a) in case 1; and \tilde{p}_t and \tilde{d}_t are cointegrated with cointegrating vector $(1 - \alpha)$.</p> <p>b. \tilde{p}_t is TS.</p> <p>c. \tilde{d}_t is TS.</p> <p>From equations (7) and (11), \tilde{d}_t will be TS if $\delta > r$.</p>	<p>a. \tilde{p}_t and \tilde{d}_t are cointegrated with cointegrating vector $(1 - \alpha)$.</p> <p>b. \tilde{m}_t and \tilde{d}_t are cointegrated with cointegrating vector $(1 - 1/\beta)$.</p> <p>c. \tilde{m}_t and \tilde{p}_t are cointegrated with cointegrating vector $(1 - \alpha/\beta)$.</p>
<p>3. Two of the three variables are TS</p>	<p>In all three cases, if a cointegration relation between these pairs of variables does not exist, attempts to estimate the import demand equation will result in a spurious regression. Hence, to detect this potential spuriousness, a residual-based cointegration test will be performed on equation (13).</p>
<p>4. All three variables are TS This is the only case in which classical inference is valid.</p>	<p>This case can be viewed as a rejection of the model, since there is no linear combination of the three variables that yields a stationary process.</p> <p>The import demand equation (13) becomes a classical regression equation with population coefficients $(1/\beta - \alpha/\beta)$.</p>

^a \tilde{p}_t is either exogenous under a perfectly elastic import supply or is endogenously determined by the interaction of the demand and supply of imports. The supply of imports is not modeled explicitly here.

^b See Stock and Watson (1988)

II. Estimation Results

The data come from the World Bank database BESD. The sample includes 77 countries for which the required data are available for a reasonable time span (the list of countries is given in Table 2). In general, the data are available from 1960 to 1993.⁸ The usual problem is of course the choice of the corresponding proxies for the variables in the model, since the model is usually a crude simplification of reality—which is the case here. Data constraints highly restrict this choice. Total imports and exports of goods and services will be used for m_t and x_t in equation (14). The relative price of imports p_t will be computed as the ratio of the import deflator to the GDP deflator.⁹ The activity variable will be computed as the difference between GDP and exports.¹⁰

Unit Root Test

The FM procedure assumes that some of the variables entering the cointegrating equation (15) have a unit root and that there exists a stationary linear combination of these variables. We tested for the existence of a unit root in all three variables in the import demand equation (15), namely, real imports of goods and services (m), the relative price of imports (p), and the activity variable GDP minus exports (gdp_x). The unit root hypothesis is tested using the Augmented-Dickey-Fuller (ADF) test. The lag length (k) in the ADF regression is selected using the Schwarz criterion (Table 2). For m_t , only 4 of the 77 countries reject the unit root at 5 percent or less (Australia at 1 percent, Nicaragua, Peru, and Philippines at 5 percent). Similarly, the null of a unit root in p_t is rejected only for 3 countries (China at 1 percent, and Papua New Guinea and Uruguay at 5 percent). Finally, as far as gdp_x_t is concerned, the unit root is rejected for 10 countries (Burundi, Central African Republic, Iceland, Switzerland, and Trinidad and Tobago at 1 percent; Korea, Rwanda, Togo, Tunisia, and Zaire at 5 percent). Thus for most of the countries, the unit root hypothesis cannot be rejected at conventional significance levels. This finding, of course, may reflect to a certain extent the low power of the ADF.

⁸The following countries have a shorter data range: Cameroon (1965–93), Ecuador (1965–93), Sudan (1960–91), Tunisia (1961–93), and Yugoslavia (1960–90).

⁹Feenstra (1994) points out the problem that these aggregate prices do not account properly for quality upgrade over time.

¹⁰Even though the behavior of imports of consumption and intermediate goods may differ, data availability precludes us from analyzing disaggregated import demand equations.

Import Demand Equations

The results underscore the presence of nonstationarity in the data and the adverse consequences of neglecting it. Table 2 shows that most countries—60 of the 77—fall into the first case of Table 1 (the unit root hypothesis cannot be rejected for all three variables in the import demand equation) and the remaining countries—17 of the 77—into the second case (the unit root hypothesis can be rejected for only one of the three variables). In the first case, the model predicts a cointegrating relationship between the three I(1) variables, and in the second case between the two I(1) variables. No country belongs to either the third or fourth cases.

Table A1 in the Appendix shows both the OLS and FM estimates of the import demand equation. Only countries with the right sign for the price and income elasticities are reported (66 of the 77 countries). The columns of Table A1 labeled x_t , p , and gdp_x give, respectively, the coefficient estimates of the lagged dependent variable (log of imports of goods and non-factor services), the short-term price elasticity (that is, the coefficient of the log of relative price of imports), and the short-term income elasticity (the coefficient of the log of gdp_x). The long-run price and income elasticities are defined, respectively, as the short-run price and income elasticities divided by one minus the coefficient estimate of the lagged dependent variable. They are given by E_p and E_y for the FM estimates.¹¹ The variance, and hence the t -statistic, for E_p and E_y are computed using the *delta method*, which consists of taking the Taylor approximation of $\text{var}(E_p)$ and $\text{var}(E_y)$:

$$\text{var}(E_p) = \left(\frac{1}{1-\gamma_1}\right)^2 \text{var}(\gamma_2) + \left[\frac{\gamma_2}{(1-\gamma_1)^2}\right]^2 \text{var}(\gamma_1) + 2\left(\frac{1}{1-\gamma_1}\right)\left[\frac{\gamma_2}{(1-\gamma_1)}\right] \text{cov}(\gamma_1, \gamma_2), \quad (16)$$

where γ_1 is the coefficient of the lagged dependent variable and γ_2 is the short-run price elasticity; $\text{var}(E_y)$ is obtained by substituting γ_2 by γ_3 in $\text{var}(E_p)$, where γ_3 is the short-run income elasticity. The column labeled *ser* reports the standard error of the regression. Finally, the column labeled *AC* gives Durbin's autocorrelation test. It amounts to estimating an AR(1) process on the estimated residuals of the import equation. Durbin's test is simply a significance test of the AR(1) coefficient using the usual t -test. For the OLS regressions, AR(1) autocorrelation is detected (at 10 percent or less) for 17 of the 66 countries.

Even though Table A1 reports both the OLS and FM estimates of the import demand equation, the discussion will focus only on the latter since

¹¹The OLS estimates of E_p and E_y are close to the FM estimates and were therefore omitted from Table A1.

Table 2. Augmented-Dickey-Fuller Test for Variables Entering the Import Demand Equation

Country	m	k	p	k	gdp	k	nobs	Country	m	k	p	k	gdp	k	nobs
1. Algeria	-0.33	1	1.08	2	-1.25	2	34	40. Korea	-1.48	1	-2.30	2	-3.76*	1	34
2. Argentina	-3.29	2	-2.04	1	-2.44	1	34	41. Madagascar	-2.92	1	-1.77	1	-2.45	1	34
3. Australia	-4.45	1	-1.71	1	-2.15	1	34	42. Malawi	-2.46	1	-1.97	1	-2.77	1	34
4. Austria	-1.77	1	-1.67	1	-1.50	1	34	43. Malaysia	-2.01	1	0.27	1	-2.38	1	34
5. Belgium Luxembourg	-1.79	1	-0.09	2	-2.08	1	34	44. Mauritania	-1.53	1	-2.50	2	-2.55	1	34
6. Benin	-0.56	2	-1.12	2	-0.89	1	34	45. Mauritius	-2.44	2	-2.22	1	-1.99	1	34
7. Brazil	-1.11	1	0.21	1	-2.64	1	34	46. Mexico	-3.47	2	-1.17	1	-1.63	1	34
8. Burundi	-3.09	1	-2.85	3	-4.46**	1	34	47. Morocco	-1.67	1	-1.41	1	-1.50	1	34
9. Cameroon	-1.28	1	0.40	1	-1.16	1	29	48. Myanmar	-1.69	1	-1.37	2	2.39	1	34
10. Canada	-2.54	1	0.69	1	-1.45	1	34	49. Netherlands	-2.22	1	-1.98	1	-2.23	1	34
11. Central African Rep.	-0.07	2	-3.17	1	-4.86**	1	34	50. New Zealand	-3.28	1	-2.37	2	-2.00	1	34
12. Chad	-2.08	1	-1.85	1	-3.34	1	34	51. Nicaragua	-3.81**	1	-1.96	1	-2.52	1	34
13. Chile	-2.00	1	-2.15	1	-2.07	2	34	52. Nigeria	-1.23	2	-2.57	1	-0.58	1	34
14. China	-1.89	1	-4.33	1	-2.40	2	34	53. Norway	-1.74	1	1.29	1	-2.47	1	34
15. Colombia	-2.17	1	-0.28	1	-1.98	1	34	54. Pakistan	-2.79	1	-2.34	2	-2.50	1	34
16. Congo	-2.10	2	-2.25	1	-2.55	2	34	55. Panama	-2.26	1	-1.69	1	-1.45	1	34
17. Costa Rica	-1.78	1	-1.04	2	-3.43	1	34	56. Papua New Guinea	-2.83	1	-3.63	3	-1.88	2	33
18. Côte d'Ivoire	-0.25	1	-2.69	1	-2.74	1	34	57. Paraguay	-2.45	1	-1.28	1	-1.97	1	34
19. Denmark	-2.11	1	-1.60	1	-1.88	1	34	58. Peru	-3.78**	2	-1.34	1	-1.65	1	34
20. Dominican Republic	-3.51	1	-1.10	1	-2.94	1	34	59. Philippines	-3.68**	2	-0.41	1	-1.67	1	34

21. Egypt	-1.21	1	-0.83	1	-2.50	2	34	60. Portugal	-2.31	1	-0.64	1	-0.60	1	34
22. El Salvador	-2.20	2	-1.80	1	-1.40	2	34	61. Rwanda	-2.31	1	-1.65	3	-3.55*	1	34
23. Finland	-1.82	1	-1.71	1	-1.40	2	34	62. South Africa	-3.18	1	0.07	1	-0.37	1	34
24. France	-2.03	1	-1.49	1	-1.62	1	34	63. Spain	-2.68	1	-1.47	1	-1.51	2	34
25. Gabon	-1.03	1	-1.31	1	-2.36	1	34	64. Sudan	-1.79	1	-1.97	1	-1.39	1	32
26. Gambia	-1.60	1	-3.06	1	-1.28	1	34	65. Sweden	-2.06	1	-0.73	1	-1.52	1	34
27. Germany	-1.87	2	-1.90	1	-1.52	1	34	66. Switzerland	-1.41	1	-2.74	1	-4.27**	2	34
28. Greece	-2.66	1	-1.19	1	0.20	1	34	67. Thailand	-1.39	1	-1.88	1	-2.00	1	34
29. Guatemala	-1.98	1	-0.81	1	-2.25	1	34	68. Togo	-0.39	1	-3.31	1	-3.62	1	34
30. Haiti	-2.83	1	0.88	1	-1.73	1	34	69. Trinidad & Tobago	-2.59	1	0.95	1	-4.35**	1	34
31. Honduras	-2.91	1	-2.62	2	-3.08	2	34	70. Tunisia	-1.32	1	-1.55	1	-3.75**	1	33
32. Iceland	-1.82	1	-0.94	2	-4.38**	3	34	71. Turkey	-1.81	1	-1.87	1	-1.40	1	34
33. India	-2.20	1	-2.16	1	-2.71	1	34	72. United Kingdom	-2.17	1	-3.48	1	-1.59	2	34
34. Indonesia	-1.88	1	-2.31	1	-1.64	1	27	73. United States	-2.34	1	-2.69	1	-0.59	1	34
35. Ireland	-2.54	1	0.04	1	-2.20	1	34	74. Uruguay	-1.89	1	-3.72	1	-2.22	2	34
36. Israel	-1.69	1	-1.97	1	-1.71	1	34	75. Yugoslavia	-1.76	1	0.25	1	-2.62	1	31
37. Italy	-2.15	1	-0.39	1	-1.10	1	34	76. Zaire	-2.56	1	-1.72	1	-4.02*	1	30
38. Japan	-2.04	1	-2.09	1	-1.54	1	34	77. Zambia	-2.09	1	-2.73	1	-2.27	1	34
39. Kenya	-2.02	1	-0.41	1	-1.25	1	34								

Notes: Variables are real imports of goods and nonfactor services (m), the real exchange rate (p), computed as the ratio of imports deflator to GDP deflator, and GDP minus exports (gdp_x). These three variables are tested for the existence of a unit root using the Augmented-Dickey-Fuller (ADF) test. The optimal lag selected by the Schwarz criterion in the ADF regression is given by k . Critical values are a linear interpolation between the critical values for $T=25$, and $T=50$ given in Hamilton (1993, Table B.6, case 4), where T is the sample size. Significance levels at 1 percent and 5 percent are indicated by two asterisks and one asterisk, respectively.

both estimation methods yield relatively close results. The short-run price elasticities vary from -0.01 (Algeria) to -0.86 (Malawi), with a sample average (over the 66 countries) of -0.26 , a median of -0.22 , and a standard deviation of 0.19 . Therefore, imports appear to be quite inelastic in the short term. The long-run price elasticities vary from -0.02 (Chile) to -6.74 (Benin). The sample average is -1.08 , the median is -0.80 , and the standard deviation is 1.08 . As expected, imports are much more responsive to relative prices in the long run than in the short run. The short-run income elasticities vary from 0.0 (Zaire) to 1.36 (Haiti). The sample average is 0.45 , the median is 0.32 , and the standard deviation is 0.34 . Thus, the average short-run income elasticity is significantly less than 1. The long-run income elasticities vary from 0.03 (Zaire) to 5.48 (Uruguay). The sample average is 1.45 , the median is 1.32 , and the standard deviation is 0.93 . Thus, imports respond much more to both relative prices and income in the long run than in the short run. E_p^c and E_y^c give the long-run price and income elasticities corrected for bias. The correction is generally small. As will be discussed in Section III, the bias is negligible when the relative price of imports and the activity variable are either exogenous or weakly endogenous, as is the case for most countries. Since unit-price and unit-income elasticities are widely used as benchmark values, a formal test for long-run unit-price and unit-income elasticities is provided in the columns labeled $E_p = -1$ and $E_y = 1$, respectively. This test uses exact critical values of the t -statistic (given in Table 5 and discussed in Section III). Fifteen of the 66 countries reject a long-run unit-price elasticity and 27 countries reject a long-run unit-income elasticity at 10 percent or less. The fit as measured by \bar{R}^2 is good.

Table 1 showed that in the first two cases, estimates of the price and income elasticities will be meaningful only if the $I(1)$ variables are cointegrated. A cointegration test is therefore required. The results of the Phillips-Ouliaris residual test of cointegration is given in Table A1 under the heading P-O. Even with a relatively small sample size (and therefore low power), the null of noncointegration is rejected for 49 of the 66 countries (at 1 percent in most cases).

An interesting question is whether the long-run income and price elasticities differ significantly between industrial and developing countries. The answer is given by the following two regressions:

$$E_y = 0.96 + 1.010 \text{ dumdc} \quad R^2 = 0.66$$

(17.49) (10.59) (17)

$$|E_p| = 0.73 - 0.316 \text{ dumdc} \quad R^2 = 0.63, \quad (18)$$

(12.03) (-3.25)

where E_p and E_y are, respectively, the long-run price and income elasticities and *dumdc* is a dummy variable that takes the value of one for an industrial and zero for a developing country. The two equations are generalized least squares (GLS) regressions of the long-run income and price elasticities on *dumdc*.¹² Industrial countries have significantly higher long-run income elasticities than developing countries (equation 17) and face much more inelastic import demand than do developing countries (equation 18).

III. Small-Sample Properties of the OLS and FM Estimators

This section analyzes the small-sample properties of the OLS and FM estimators by deriving the exact bias of the short- and long-run elasticities as well as the distribution of their *t*-statistic, which are crucial for conducting inference. The Monte Carlo derivation of these small sample properties are described in detail in each table.

Bias of the Short- and Long-Run Elasticities

Table 3 shows the bias for the OLS and the FM estimates of the short- and long-run price and income elasticities varies significantly with the degree of endogeneity of the explanatory variables (see Table 3), that is, with the correlation between the innovations in the import demand equation and the innovations in the relative price of imports (R_{12}), and the correlation between the innovations in the import demand equation and the innovations in the activity variable (R_{13}). The FM bias reaches its minimum when $R_{12} = R_{13} = 0$ and equals -0.37 percent, 0.99 percent, and -1.14 percent for the dependent variable and for the short-run price and income elasticities, respectively. This implies that both the short-run price and income elasticities are underestimated, the former by 0.99 percent and the latter by 1.14 percent.¹³ The corresponding OLS figures are -3.79 percent and 3.69 percent. The OLS

¹²The variance-covariance matrix in the GLS estimation is constructed using the FM estimates of the variances of the income and price elasticities for each country. The R^2 is computed using Buse's (1973) method, which yields a properly normalized statistic for GLS residuals.

¹³Because the price elasticity is negative while the income elasticity is positive, these elasticities are underestimated if the price elasticity bias is positive and the income elasticity bias is negative.

Table 3. Bias for Short- and Long-Run Elasticities for OLS and FM Estimators
(in percent)

		Short-Run Price and Income Elasticities											
		OLS						FM					
		$R_{12} = -0.7$	$R_{13} = -0.3$	$R_{13} = 0$	$R_{13} = 0.3$	$R_{13} = 0.7$	$R_{13} = -0.7$	$R_{13} = -0.3$	$R_{13} = 0$	$R_{13} = 0.3$	$R_{13} = 0.7$		
$R_{12} = -0.7$	α_1	6.25	-2.41	-12.45	-23.32	-33.24	5.32	-0.84	-9.10	-19.31	-29.56		
	α_2	-19.98	-35.47	-47.91	-67.94	-79.06	-1.46	-15.11	-30.47	-52.68	-70.07		
	α_3	-20.70	-4.56	14.65	37.19	59.93	-15.80	-3.09	13.89	35.89	58.90		
$R_{12} = -0.3$	α_1	9.48	2.13	-6.75	-13.64	-25.07	8.59	3.50	-3.54	-9.76	-20.70		
	α_2	2.44	-3.85	-21.65	-24.48	-40.87	12.75	5.05	-10.80	-19.25	-38.61		
	α_3	-23.88	-9.44	8.02	24.44	48.76	-21.60	-10.57	4.27	18.80	43.07		
$R_{12} = 0$	α_1	11.32	3.48	-3.07	-10.25	-21.78	10.13	4.68	-0.37	-6.40	-17.37		
	α_2	12.43	3.45	-3.79	-11.97	-26.02	18.96	9.49	0.99	-8.89	-27.40		
	α_3	-25.68	-10.08	3.69	18.99	43.80	-24.29	-12.57	-1.14	12.52	36.91		
$R_{12} = 0.3$	α_1	13.77	6.71	0.16	-8.69	-19.84	11.86	7.04	2.10	-5.40	-15.73		
	α_2	22.67	14.15	12.65	-3.53	-12.78	24.64	16.53	10.65	-4.65	-19.15		
	α_3	-28.04	-14.22	-0.10	18.04	41.55	-26.99	-16.25	-5.26	11.12	34.12		
$R_{12} = 0.7$	α_1	17.80	12.34	3.85	-7.63	-18.80	14.21	10.57	4.33	-5.15	-15.54		
	α_2	43.20	41.79	32.29	25.67	11.98	34.99	30.78	20.44	8.66	-7.34		
	α_3	-31.59	-20.05	-4.34	16.94	39.61	-30.64	-21.97	-8.70	11.41	34.04		

Long-Run Price and Income Elasticities

		OLS					FM				
		$R_{13} = -0.7$	$R_{13} = -0.3$	$R_{13} = 0$	$R_{13} = 0.3$	$R_{13} = 0.7$	$R_{13} = -0.7$	$R_{13} = -0.3$	$R_{13} = 0$	$R_{13} = 0.3$	$R_{13} = 0.7$
$R_{12} = -0.7$	E_p	-43.29	-30.50	-15.83	-9.54	-1.22	-16.11	-13.53	-8.26	-5.81	-0.86
	E_y	-3.60	-6.93	-9.76	-10.39	-9.57	-2.63	-3.42	-4.88	-5.60	-5.70
$R_{12} = -0.3$	E_p	-27.18	-10.70	-6.21	4.71	10.52	-9.95	-4.60	-3.43	1.84	5.82
	E_y	0.10	-3.01	-5.36	-4.70	-5.55	-0.69	-1.05	-2.26	-2.13	-2.87
$R_{12} = 0$	E_p	-20.58	-6.37	1.81	8.58	15.70	-7.08	-2.91	0.27	3.91	8.47
	E_y	3.24	-0.48	-1.86	-2.88	-3.93	0.48	-0.15	-0.41	-0.80	-1.87
$R_{12} = 0.3$	E_p	-15.83	-3.14	10.65	12.69	21.80	-5.23	-1.26	4.27	5.70	11.68
	E_y	7.98	3.15	1.78	-0.62	-2.25	2.03	1.63	1.12	-0.07	-1.06
$R_{12} = 0.7$	E_p	-0.13	15.55	23.05	34.38	36.98	2.01	6.76	9.64	16.52	19.82
	E_y	14.35	14.63	7.32	1.44	-1.33	4.27	4.58	2.85	0.64	-0.84

Notes: The bias is generated by simulating the import demand model: $m_t = \alpha_1 m_{t-1} + \alpha_2 p_t + \alpha_3 gdp_x_t + \epsilon_{1t}$, $p_t = p_{t-1} + \epsilon_{2t}$, and $gdp_x_t = gdp_{x,t-1} + \epsilon_{3t}$, $(\epsilon_{1t}, \epsilon_{2t}, \epsilon_{3t}) \sim N(0, \Sigma)$ and $\text{corr}(\epsilon_{1t}, \epsilon_{2t}, \epsilon_{3t}) = R_{ij}$, $i, j = 1, 2, 3$, where m_t denotes imports, p_t is the real exchange rate and gdp_x_t is the activity variable that is GDP-exports. All variables are in logs. The coefficients α_1 , α_2 , and α_3 are set to 0.70, -1.00 and 1.00 respectively. The long-run elasticities are defined as $E_p = \alpha_2 / (1 - \alpha_1)$ and $E_y = \alpha_3 / (1 - \alpha_1)$. The empirical distribution of the elasticities is generated from 5,000 drawings of 34 observations each (the sample size in the data) from the import demand model. For each drawing, the import demand model is estimated. This yields 5,000 estimates of the short- and long-run elasticities. For each drawing, the bias is simply the difference between the elasticity estimate and its true value. The table reports the mean of these biases expressed in percent of the true elasticities. The bias is computed for 5 different values of R_{12} (the correlation between ϵ_{1t} and ϵ_{2t}) and 5 different values of R_{13} (the correlation between ϵ_{1t} and ϵ_{3t}). This yields 25 bias distributions for each elasticity.

bias is generally much higher than the corresponding FM one. Note that for this benchmark case (where $R_{12} = R_{13} = 0$), OLS differs from FM both in the magnitude and in the direction of the bias. Negative values of R_{12} tend to bias both the price and the income elasticities downward while positive ones induce an upward bias. Negative values of R_{13} tend to bias both the price and the income elasticities upward while positive values induce a downward bias. The bias becomes substantial for high values of R_{12} and R_{13} .

Because long-run elasticities depend not only on the short-run elasticities (α_1 and α_2) but also on the adjustment speed as measured by the coefficient on the lagged dependent variable (α_1), the bias in the short-run elasticities does not translate one-for-one to the long-run elasticities. The OLS bias is generally much higher than the corresponding FM one. When $R_{12} = R_{13} = 0$, the FM bias still reaches its minimum for the price elasticity (0.27 percent) but is slightly higher than the minimum for the income elasticity (-0.41 percent). The corresponding OLS figures are 1.81 percent and -86 percent. These values imply that both the long-run price and income elasticities are underestimated. Negative values of R_{12} tend to bias both long-run elasticities upward, while positive values have the opposite effect. Negative values of R_{13} induce an upward bias in the long-run price elasticity and a downward bias in the long-run income elasticity. The reverse holds for positive values of R_{13} . Interestingly, the bias on the long-run elasticities is generally lower than the bias on the short-run elasticities.

Exact Distribution of the t -Statistic

For the benchmark case in which both explanatory variables are assumed to be exogenous ($R_{12} = R_{13} = 0$), the small-sample t -distribution for the imports relative price (p) and the activity variable (gdp_x) are symmetric but are wider than the asymptotic t -distribution (Table 4). For reference, the asymptotic critical values of the t -distribution at 1 percent, 5 percent, and 10 percent are -2.33, -1.65, and -1.28, respectively. The corresponding small-sample critical values are -3.13, -2.06, and -1.61 for p , and -3.20, -2.15, and -1.64 for gdp_x . The t -distribution of the lagged dependent variable (m_{t-1}) is skewed to the left, as expected, since m_t has a unit root. When p is allowed to be endogenous (that is, $R_{12} \neq 0$), the distribution of its t -statistic becomes skewed, while the t -statistic distribution of gdp_x becomes flatter. Similarly, when gdp_x is allowed to be endogenous (that is, $R_{13} \neq 0$), the distribution of its t -statistic becomes skewed, while the t -statistic distribution of p becomes flatter. The stronger the endogeneity of p or gdp_x , that is, the larger (in absolute value) R_{12} or R_{13} , the larger is this departure from the asymptotic t -distribution.

For the benchmark case $R_{12} = R_{13} = 0$, the t -distributions of E_p (the long-run price elasticity) and E_y (the long-run income elasticity) are symmetric but flatter than the asymptotic t -distribution (Table 5). The 1 percent, 5 percent, and 10 percent critical values are -3.38 , -2.14 , and -1.60 for E_p , and -3.65 , -2.22 , and -1.69 for E_y . As for the short-run elasticity, when p is allowed to be endogenous, the t -statistic distribution of E_p becomes skewed, while the t -statistic distribution of E_y becomes flatter. Similarly, when gdp_x is allowed to be endogenous, the t -statistic distribution of E_y becomes skewed, while the t -statistic distribution of E_p becomes flatter. The stronger the endogeneity, the larger is the deviation from the asymptotic t -distribution.

IV. Conclusions

Despite the stringent constraints imposed by data availability, which dictated both the level of aggregation and the simplicity of the model, this analysis provides the applied researcher with some interesting insights.

- The paper offers a wide range of income and price elasticities for both industrial and developing countries, estimated within a consistent framework using recent time series techniques that address nonstationarity in the data.
- The long-run price and income elasticities for a large majority of countries have the expected sign and, in most cases, are statistically significant. Imports react relatively slowly to movements in their relative price and in the activity variable. Industrial countries tend to have significantly higher income elasticities and lower price elasticities than developing countries.
- The bias and the distribution of the t -statistic are shown to depend critically on the degree of endogeneity of the explanatory variables. It is shown that inference conducted on the basis of the usual asymptotic t - or F -distributions may be very misleading.

A similar framework can be used for the estimation of the export demand elasticities. This is the object of ongoing research.

Table 4. FM t-Statistic Critical Values for the Parameters of the Import Demand Equation

	$R_{13} = -0.7$		$R_{13} = -0.3$		$R_{13} = 0$		$R_{13} = 0.3$		$R_{13} = 0.7$					
	m_{-1}	p	m_{-1}	p	m_{-1}	p	m_{-1}	p	m_{-1}	p				
1%	-1.85	-3.28	-3.65	-3.68	-6.05	-5.94	-4.22	-4.11	-9.48	-5.15	-3.01	-18.27	-6.29	-1.41
5%	-0.48	-2.29	-2.45	-2.72	-4.40	-4.51	-3.08	-2.87	-7.92	-3.80	-1.75	-15.84	-4.79	-0.05
10%	0.20	-1.83	-1.82	-2.20	-3.52	-3.88	-2.49	-2.23	-7.17	-3.15	-1.17	-14.57	-4.06	0.53
$R_{12} = -0.7$														
90%	6.18	0.51	-0.49	2.52	0.73	1.13	0.82	2.09	-2.81	0.75	3.45	-8.76	0.13	5.59
95%	7.01	0.82	0.11	3.14	1.10	1.72	0.49	1.28	-2.26	1.24	4.25	-8.18	0.85	6.58
99%	8.77	1.47	1.10	4.42	1.87	2.88	1.41	2.09	-1.34	2.29	6.04	-7.06	2.24	8.71
1%	0.05	-2.97	-5.51	-1.86	-3.11	-4.03	-3.95	-3.69	-5.54	-3.74	-2.79	-9.41	-4.41	-2.23
5%	1.13	-2.07	-3.84	-0.86	-2.11	-2.84	-2.70	-2.40	-4.37	-2.52	-1.82	-7.80	-2.96	-1.23
10%	1.75	-1.58	-3.20	-0.32	-1.66	-2.22	-2.15	-1.94	-3.72	-2.02	-1.31	-7.02	-2.38	-0.78
$R_{12} = -0.3$														
90%	6.05	1.18	0.72	3.36	1.39	1.28	1.29	1.33	-0.18	1.48	2.17	-2.78	1.61	3.12
95%	6.77	1.60	1.34	3.93	1.84	1.83	1.74	1.81	0.25	2.04	2.77	-2.31	2.19	3.88
99%	8.09	2.41	2.36	4.78	2.64	2.75	2.58	2.81	1.12	3.09	4.02	-1.42	3.40	5.43
1%	0.88	-2.65	-4.62	-1.38	-2.99	-3.62	-2.95	-3.13	-4.67	-3.27	-2.83	-8.27	-3.80	-2.15
5%	1.95	-1.81	-3.39	-0.45	-1.98	-2.51	-1.83	-2.06	-3.51	-2.28	-1.76	-6.57	-2.62	-1.28
10%	2.52	-1.41	-2.77	0.10	-1.55	-2.00	-1.34	-1.61	-2.83	-1.74	-1.32	-5.87	-1.98	-0.83

$R_{12} = 0$	6.68	1.34	0.75	3.54	1.50	1.28	2.04	1.64	1.68	0.68	1.77	1.97	-1.83	1.96	2.71
90%	7.30	1.75	1.17	4.11	1.96	1.69	2.51	2.14	2.13	1.15	2.30	2.55	-1.29	2.59	3.40
95%	8.73	2.58	2.06	5.23	2.97	2.64	3.43	3.17	3.14	1.88	3.42	3.73	-0.46	3.75	4.86
99%	2.20	-2.39	-4.44	-0.59	-2.66	-3.55	-2.20	-2.83	-3.02	-4.32	-3.05	-2.45	-7.80	-3.29	-2.07
1%	3.37	-1.65	-3.09	0.47	-1.72	-2.39	-1.21	-1.75	-2.02	-3.20	-2.08	-1.64	-6.16	-2.15	-1.26
5%	3.90	-1.20	-2.48	1.00	-1.26	-1.90	-0.71	-1.31	-1.48	-2.61	-1.59	-1.20	-5.51	-1.54	-0.85
10%	8.17	1.58	0.82	4.68	1.73	1.17	2.75	1.96	1.47	0.87	1.96	1.89	-1.46	2.43	2.57
$R_{12} = 0.3$	8.81	2.01	1.23	5.24	2.19	1.61	3.30	2.48	1.95	1.30	2.49	2.46	-0.96	3.12	3.17
90%	10.43	2.82	2.03	6.46	3.17	2.56	4.30	3.44	2.94	2.27	3.61	3.42	-0.07	4.40	4.44
95%	5.52	-1.52	-4.21	1.32	-1.81	-3.13	-1.65	-2.25	-2.56	-4.93	-2.24	-2.10	-9.59	-2.21	-1.50
99%	7.44	-0.80	-2.74	2.58	-1.14	-2.17	-0.59	-1.27	-1.70	-3.60	-1.24	-1.40	-7.92	-0.93	-0.78
1%	8.21	-0.48	-2.17	3.21	-0.77	-1.68	-0.05	-0.80	-1.30	-2.98	-0.71	-1.01	-7.13	-0.27	-0.47
5%	13.66	1.83	0.51	7.80	2.18	1.03	4.06	2.50	1.29	1.20	3.06	1.66	-2.15	4.05	2.21
10%	14.57	2.25	0.80	8.47	2.68	1.40	4.69	3.07	1.72	1.86	3.68	2.14	-1.40	4.73	2.80
$R_{12} = 0.7$	16.39	3.25	1.46	9.89	3.82	2.18	5.92	4.30	2.55	3.03	5.13	3.11	-0.20	6.42	4.16
90%															
95%															
99%															

Notes: This table provides exact critical values of the FM t -statistic at 1%, 5%, 10%, 90%, 95% and 99% significance levels. These critical values are generated by simulating the import demand model: $m_t = \alpha_1 m_{t-1} + \alpha_2 p_t + \alpha_3 gdp_t + \varepsilon_{1t}$, $p_t = p_{t-1} + \varepsilon_{2t}$ and $gdp_t = gdp_{t-1} + \varepsilon_{3t}$, $(\varepsilon_{1t}, \varepsilon_{2t}, \varepsilon_{3t}) \sim N(0, \Sigma)$ and $\text{corr}(\varepsilon_{1t}, \varepsilon_{2t}, \varepsilon_{3t}) = R_{ij}$, $i, j = 1, 2, 3$; m_t denotes imports, p_t is the real exchange rate, and gdp_t is the activity variable that is GDP-exports. All variables are in logs. The coefficients α_1, α_2 and α_3 are set to 0.70, -1.00 and 1.00, respectively. For each of the coefficients, the critical values are computed by (1) setting the coefficient for which the critical values are computed to zero (restricted model), (2) drawing 5,000 samples of 34 observations each (the sample size in the data) from the restricted model, (3) computing the usual t -statistic for each drawing, and (4) using the resulting vector of 5,000 t -statistic values to generate an empirical distribution from which the critical values can be computed. For each coefficient, the empirical t -distribution is computed for 5 different values of R_{12} (the correlation between ε_{1t} and ε_{2t}) and 5 different values of R_{13} (the correlation between ε_{1t} and ε_{3t}). This yields 25 empirical t -distributions for each of the three coefficients.

Table 5. FM t-Statistic Critical Values for Long-Run Import Price and Income Elasticities

		$R_{13} = -0.7$			$R_{13} = -0.3$			$R_{13} = 0$			$R_{13} = 0.3$			$R_{13} = 0.7$		
		E_p	E_y	E_p	E_y	E_p	E_y	E_p	E_y	E_p	E_y	E_p	E_y	E_p	E_y	
$R_{12} = -0.7$	1%	-3.39	-9.95	-4.02	-6.81	-4.83	-4.41	-5.81	-3.08	-7.01	-1.40					
	5%	-2.24	-7.40	-2.77	-4.77	-3.26	-2.99	-4.08	-1.79	-5.14	-0.05					
	10%	-1.81	-6.23	-2.21	-3.71	-2.57	-2.28	-3.32	-1.19	-4.32	0.53					
	90%	0.50	-0.49	0.72	1.12	0.82	2.12	0.75	3.62	0.13	6.16					
	95%	0.80	0.11	1.09	1.69	1.25	2.80	1.26	4.57	0.86	7.26					
	99%	1.36	1.12	1.79	3.01	2.14	4.37	2.35	6.86	2.33	9.81					
	1%	-3.03	-6.78	-3.24	-4.94	-3.98	-3.80	-4.09	-2.82	-4.91	-2.25					
	5%	-1.97	-4.44	-2.07	-3.01	-2.53	-2.44	-2.67	-1.77	-3.16	-1.22					
	10%	-1.55	-3.53	-1.67	-2.36	-1.97	-1.85	-2.06	-1.29	-2.48	-0.77					
$R_{12} = -0.3$	90%	1.15	0.70	1.34	1.29	1.31	1.84	1.50	2.31	1.63	3.41					
	95%	1.52	1.28	1.81	1.83	1.80	2.49	2.05	3.00	2.25	4.41					
	99%	2.27	2.34	2.70	2.94	2.85	3.94	3.24	4.54	3.76	6.92					
	1%	-2.57	-5.91	-3.07	-4.21	-3.38	-3.65	-3.54	-3.08	-4.23	-2.14					
	5%	-1.75	-3.90	-1.97	-2.73	-2.14	-2.22	-2.36	-1.77	-2.72	-1.25					
	10%	-1.34	-3.05	-1.52	-2.06	-1.60	-1.69	-1.76	-1.30	-2.02	-0.81					
	90%	1.30	0.73	1.46	1.25	1.65	1.70	1.77	2.06	1.99	3.04					
	95%	1.68	1.11	1.98	1.68	2.16	2.25	2.38	2.79	2.69	3.95					
	99%	2.48	2.02	2.89	2.76	3.32	3.63	3.61	4.35	4.11	6.25					
$R_{12} = 0$	1%	-2.22	-5.53	-2.56	-4.33	-2.78	-3.35	-3.28	-2.59	-3.53	-2.02					
	5%	-1.51	-3.63	-1.72	-2.57	-1.76	-2.08	-2.13	-1.57	-2.21	-1.21					
	10%	-1.14	-2.73	-1.24	-1.95	-1.27	-1.49	-1.58	-1.17	-1.58	-0.82					

$R_{12} = 0.3$												
90%	1.52	0.80	1.68	1.15	1.98	1.49	2.04	1.94	2.52	2.80		
95%	1.91	1.21	2.20	1.57	2.56	2.00	2.61	2.61	3.32	3.77		
99%	2.75	2.02	3.27	2.46	3.70	3.38	3.90	4.11	4.91	5.80		
1%	-1.38	-5.92	-1.72	-3.97	-2.23	-2.89	-2.34	-2.27	-2.36	-1.38		
5%	-0.77	-3.22	-1.10	-2.40	-1.25	-1.71	-1.25	-1.34	-0.95	-0.76		
10%	-0.47	-2.38	-0.76	-1.73	-0.80	-1.26	-0.72	-0.98	-0.27	-0.47		
$R_{12} = 0.7$												
90%	1.79	0.50	2.17	0.99	2.58	1.26	3.25	1.70	4.32	2.43		
95%	2.24	0.78	2.76	1.35	3.23	1.74	4.03	2.28	5.19	3.24		
99%	3.28	1.41	4.22	2.33	4.98	2.85	6.01	3.75	7.30	5.65		

Notes: This table provides exact critical values of the FM t -statistic at 1%, 5%, 10%, 90%, 95%, and 99% significance levels for long-run import price and income elasticities (E_p and E_y , respectively). These critical values are generated by simulating the import demand model: $m_t = \alpha_1 m_{t-1} + \alpha_2 p_t + \alpha_3 gdp_t + \varepsilon_{1t}$, $p_t = p_{t-1} + \varepsilon_{2t}$, and $gdp_t = gdp_{t-1} + \varepsilon_{3t}$, $(\varepsilon_{1t}, \varepsilon_{2t}, \varepsilon_{3t}) \sim N(0, \Sigma)$ and $\text{corr}(\varepsilon_{1t}, \varepsilon_{2t}, \varepsilon_{3t}) = R_{ij}$, $i, j = 1, 2, 3$; m_t denotes imports, p_t is the real exchange rate and gdp_t is the activity variable that is GDP-exports. All variables are in logs. The coefficients α_1, α_2 and α_3 are set to 0.70, -1.00 and 1.00, respectively. The long-run elasticities are defined as $E_p = \alpha_2 / (1 - \alpha_1)$ and $E_y = \alpha_3 / (1 - \alpha_1)$. Their respective t -statistic critical values are computed by (1) setting α_2 and α_3 equal to zero (restricted model), (2) drawing 5,000 samples of 34 observations each (the sample size in the data) from the restricted model, (3) computing the usual t -statistic for E_p and E_y using the *delta method* formula for each drawing, and (4) using the resulting vector of 5,000 t -statistic values to generate an empirical distribution from which the critical values can be computed. For both E_p and E_y , the empirical t -distribution is computed for 5 different values of R_{12} (the correlation between ε_{1t} and ε_{2t}) and 5 different values of R_{13} (the correlation between ε_{1t} and ε_{3t}). This yields 25 empirical t -distributions for both long-run elasticities.

APPENDIX

The Fully Modified Estimator

Assume that the generating mechanism for y_t is the following cointegrating system:

$$y_{1t} = \alpha_0 + \alpha_1 + \beta' y_{2t} + u_{1t} = \gamma' z_t + u_{1t} \quad (\text{A1})$$

$$\Delta y_{2t} = u_{2t} \quad (\text{A2})$$

$$u_t = \begin{pmatrix} u_{1t} \\ u_{2t} \end{pmatrix} = \Psi(L) \varepsilon_t, \quad E(\varepsilon_t \varepsilon_t') = P P', \quad (\text{A3})$$

where y_{1t} and y_{2t} are scalar and $m \times 1$ vector of $I(1)$ stochastic processes, $\gamma' = (\alpha_0 \alpha_1 \beta')$ and $z_t = (1t y_{2t})$. Define

$$\Omega = \Psi(1)P, \quad \Sigma = \Omega \Omega' = \begin{pmatrix} \Sigma_{11} & \Sigma_{21}' \\ \Sigma_{21} & \Sigma_{22} \end{pmatrix}. \quad (\text{A4})$$

Σ is the long-run covariance matrix of u_t . The FM estimator is an optimal single-equation method based on the use of OLS on equation (A1) with semiparametric corrections for serial correlation and potential endogeneity of the right-hand side variables. The method was developed in Phillips and Hansen (1990) and generalized to include deterministic trends by Hansen (1992).

Define the OLS estimator of the cointegrating equation (A1) by $\hat{\gamma} = (Z_t' Z_t)^{-1} Z_t' Y_{1t}$, where Z_t and Y_{1t} are (respectively) $T \times (m+2)$ and $T \times 1$ matrices of observations on z_t and y_{1t} . In general, $\hat{\gamma}$ is *consistent* but *biased* because of serial correlation in u_{1t} and endogeneity of y_{2t} . The idea in the FM procedure is to modify the OLS estimator $\hat{\gamma}$ to correct for serial correlation and endogeneity bias. The FM estimator is given by

$$\hat{\gamma}^{++} = \begin{pmatrix} \hat{\alpha}_0^{++} \\ \hat{\alpha}_1^{++} \\ \hat{\beta}^{++} \end{pmatrix} = \begin{pmatrix} T & \sum_{t=1}^T y_{2t}' & \sum_{t=1}^T t \\ \sum_{t=1}^T t & \sum_{t=1}^T t y_{2t}' & \sum_{t=1}^T t^2 \\ \sum_{t=1}^T y_{2t} & \sum_{t=1}^T y_{2t} y_{2t}' & \sum_{t=1}^T y_{2t} t \end{pmatrix}^{-1} \begin{pmatrix} \sum_{t=1}^T \hat{y}_{1t}^+ \\ \sum_{t=1}^T t \hat{y}_{1t}^+ \\ \sum_{t=1}^T y_{2t} \hat{y}_{1t}^+ - T \hat{V}_T^+ \end{pmatrix} \quad (\text{A5})$$

$$\hat{y}_{1t}^+ = y_{1t} - \hat{\Sigma}_{21}' \hat{\Sigma}_{22}^{-1} \Delta y_{2t} \quad (\text{A6})$$

$$\hat{\Sigma} = \begin{pmatrix} \hat{\Sigma}_{11} & \hat{\Sigma}_{21}' \\ \hat{\Sigma}_{21} & \hat{\Sigma}_{22} \end{pmatrix} = \hat{\Gamma}_0 + \sum_{v=1}^q \left(1 - \frac{v}{q+1}\right) (\hat{\Gamma}^v + (\hat{\Gamma}^v + (\hat{\Gamma}^v)')) \quad (\text{A7})$$

$$\hat{\Gamma}_v = T^{-1} \sum_{t=v+1}^T \begin{pmatrix} \hat{u}_{1t} \hat{u}_{1t-v} & \hat{u}_{1t} \hat{u}_{2t-v}' \\ \hat{u}_{2t} \hat{u}_{1t-v} & \hat{u}_{2t} \hat{u}_{2t-v}' \end{pmatrix} = \begin{pmatrix} \hat{\Gamma}_{11}^v & \hat{\Gamma}_{12}^v \\ \hat{\Gamma}_{21}^v & \hat{\Gamma}_{22}^v \end{pmatrix} \quad (\text{A8})$$

$$\hat{V}_T^+ = \sum_{v=1}^q \left(1 - \frac{v}{q+1}\right) [(\hat{\Gamma}_{12}^v)' + (\hat{\Gamma}_{22}^v)'], \quad (\text{A9})$$

where q is the bandwidth parameter in the Bartlett window used in the estimation of the long-run covariance matrix Σ by the method given in Andrews and Monahan (1991). The difference between the OLS estimator and the FM estimator is highlighted in the last vector of equation (A5) where y_{1t} is replaced by \hat{y}_{1t}^+ (which corrects for the potential endogeneity of y_{2t}) and the factor $T\hat{V}_T^+$ (which corrects for the potential autocorrelation of the error term). These two transformations are sufficient to remove the bias induced by autocorrelation of u_{1t} and the endogeneity of y_{2t} . The FM estimator $\hat{\gamma}^{++}$ has the same asymptotic behavior as the full systems maximum likelihood estimators.¹⁴

¹⁴ For more details, see Phillips and Hansen (1990), Phillips and Loretan (1991) and Hansen (1992).

Table A1. Import Demand Equations

	OLS estimates						FM estimates						nobs					
	m_{-1}	p	gdp_x	AC	ser	R^2	m_{-1}	p	gdp_x	E_p	E_y	E_p^c		ser	R^2	$P-O$	$E_p = -1$	$E_y = 1$
1. Algeria	0.81	-0.06	0.16	0.45	0.15	0.92	0.87	-0.01	0.11	-0.08	0.83	0.84	0.07	0.91	-3.66	1.73	-0.73	34
	7.71	-0.41	1.73	2.65			16.14	-0.14	2.23	-0.14	3.66 ^a							
2. Argentina	0.42	-0.64	0.80	0.19	0.16	0.80	0.42	-0.68	0.70	-1.17	1.21	1.27	0.12	0.80	-5.24 ^a	-0.85	1.12	34
	3.50	-5.00	4.57	1.01			4.71	-6.96	5.25	-5.99 ^a	6.38 ^a							
3. Australia	0.49	-0.34	0.70	0.25	0.07	0.98	0.82	-0.12	0.21	-0.66	1.19	1.22	0.08	0.97	-10.822 ^a	0.28	0.52	34
	3.93	-1.78	3.81	1.34			5.57	-0.55	0.95	-0.54	3.22 ^b							
4. Austria	0.76	-0.33	0.48	-0.07	0.04	1.00	0.82	-0.27	0.32	-1.50	1.76	1.77	0.03	1.00	-5.55 ^a	-1.19	2.25	34
	10.02	-2.20	2.64	-0.36			14.11	-2.39	2.23	-3.55 ^a	5.23 ^a							
5. Belgium-Luxembourg	0.95	-0.17	-0.04	-0.09	0.05	0.99	0.96	-0.11	0.00	-2.57	0.10	0.10	0.03	0.99	-5.45 ^a	-1.14	-0.76	34
	57.15	-1.96	-0.59	-0.44			76.91	-1.86	0.09	-1.86 ^b	0.08							
6. Benin	0.90	-0.54	0.37	0.07	0.14	0.93	0.93	-0.47	0.34	-6.74	4.91	4.83	0.08	0.94	-4.77 ^a	-1.68	1.39	34
	16.68	-1.58	1.04	0.43			29.26	-2.29	1.61	-1.97 ^b	1.74 ^b							
7. Brazil	0.83	-0.30	0.19	0.31	0.12	0.96	0.84	-0.29	0.20	-1.73	1.24	1.25	0.07	0.96	-4.35 ^b	-0.95	1.41	34
	8.17	-2.78	1.64	1.71			12.97	-4.16	2.72	-2.24 ^c	7.26 ^a							
8. Burundi	0.63	-0.27	0.55	-0.10	0.11	0.96	0.81	-0.19	0.31	-0.99	1.63	1.60	0.07	0.96	-6.10 ^a	0.01	1.58 ^c	34
	5.16	-1.29	3.46	-0.52			10.20	-1.44	2.83	-1.23	4.09 ^a							
9. Cameroon	-0.01	-0.76	1.02	0.28	0.08	0.96	0.10	-0.69	0.91	-0.77	1.01	1.00	0.07	0.96	-3.88 ^c	1.95	0.24	29
	-0.05	-3.91	5.71	1.40			0.72	-4.23	6.07	-6.53 ^a	25.24 ^a							

10. Canada	0.53 4.36	-0.57 -3.14	0.72 3.76	0.19 0.90	0.05 0.99	0.58 7.27	-0.54 -4.78	0.63 4.78	-1.28 -8.00 ^a	1.48 16.56 ^a	-1.33	1.49	0.03	0.99	-4.11 ^a	-1.77	5.35 ^a	34
11. Chile	0.26 2.14	-0.09 -1.29	1.41 6.63	0.42 2.74	0.11 0.93	0.37 2.95	-0.01 -0.14	1.18 5.21	-0.02 -0.14	1.87 10.47 ^a	-0.01	1.94	0.12	0.93	-3.79	8.66 ^a	4.89 ^a	34
12. China	0.76 9.73	-0.19 -1.00	0.53 3.15	0.41 2.54	0.19 0.98	0.89 10.99	-0.04 -0.24	0.24 1.39	-0.39 -0.26	2.16 2.50 ^a	-0.39	2.12	0.17	0.97	-3.78	0.39	1.34	34
13. Colombia	0.32 1.37	-0.63 -2.35	0.76 3.06	0.25 1.03	0.13 0.93	0.46 2.54	-0.44 -2.09	0.59 3.04	-0.80 -2.38 ^b	1.09 13.38 ^a	-0.78	1.09	0.10	0.92	-3.02	0.59	1.13	34
14. Congo	0.60 4.01	-0.42 -2.21	0.36 2.31	0.41 2.33	0.15 0.81	0.71 6.21	-0.29 -2.02	0.25 2.16	-1.02 -2.27 ^b	0.87 3.82 ^a	-1.02	0.88	0.11	0.81	-3.43	-0.03	-0.56	34
15. Costa Rica	0.74 8.01	-0.55 -5.90	0.38 2.48	0.15 0.82	0.08 0.98	0.86 10.35	-0.57 -6.81	0.16 1.16	-4.18 -1.67	1.21 3.09 ^a	-3.99	1.22	0.07	0.98	-5.08 ^a	-1.27	0.53	34
16. Côte d'Ivoire	0.67 7.58	-0.46 -2.93	0.32 3.55	0.24 1.85	0.10 0.95	0.67 8.43	-0.34 -2.40	0.32 3.78	-1.04 -2.24 ^b	0.96 6.86 ^a	-0.96	0.96	0.09	0.96	-3.91 ^c	-0.08	-0.26	34
17. Denmark	0.48 5.26	-0.14 -1.72	0.89 4.78	0.05 0.29	0.04 0.99	0.58 6.84	-0.14 -1.93	0.69 4.04	-0.34 -2.05 ^c	1.63 11.98 ^a	-0.33	1.67	0.04	0.99	-5.45 ^a	3.98 ^a	4.64 ^a	34
18. Dominican Rep.	0.30 1.89	-0.32 -1.95	0.69 3.90	0.16 0.93	0.16 0.90	0.51 3.51	-0.15 -0.98	0.43 2.63	-0.30 -1.02	0.86 5.95 ^a	-0.30	0.85	0.15	0.90	-5.72 ^a	2.36 ^c	-0.96	34
19. El Salvador	0.54 4.46	-0.49 -3.39	0.71 3.86	0.39 2.28	0.10 0.91	0.66 5.66	-0.42 -3.05	0.50 2.74	-1.23 -2.01 ^c	1.47 5.65 ^a	-1.19	1.50	0.10	0.90	-3.75	-0.38	1.79	34
20. France	0.41 4.11	-0.22 -3.61	1.21 5.41	-0.18 -1.04	0.04 1.00	0.50 7.67	-0.20 -5.50	1.02 6.95	-0.40 -4.65 ^a	2.02 45.69 ^a	-0.42	2.03	0.02	1.00	-6.78 ^a	6.85 ^a	23.05 ^a	34

Table A1. (continued)

	OLS estimates						FM estimates						<i>nobs</i>				
	<i>m</i> ₋₁	<i>p</i>	<i>gdp</i> _x	<i>AC</i>	<i>ser</i>	<i>R</i> ²	<i>m</i> ₋₁	<i>p</i>	<i>gdp</i> _x	<i>E_p</i>	<i>E_y</i> ^c	<i>ser</i>		<i>R</i> ²	<i>P-O</i>	<i>E_p</i> = -1	<i>E_y</i> = 1
41. Myanmar	0.81 7.48	-0.04 -0.37	0.08 0.74	0.16 0.80	0.21 0.80	0.63	0.90 14.28	-0.06 -0.97	0.01 0.15	-0.57 -0.83	0.09 0.15	0.09	0.61	-4.67 ^a	0.61	-1.49	34
42. New Zealand	0.42 3.45	-0.38 -4.11	1.12 4.54	0.14 0.72	0.07 0.72	0.96	0.60 4.81	-0.32 -3.54	0.84 3.21	-0.80 -3.72 ^a	2.11 10.55 ^a	2.08	0.96	-5.21 ^a	0.94	5.54 ^a	34
43. Nicaragua	0.40 2.68	-0.15 -1.47	0.36 2.00	0.12 0.69	0.18 0.69	0.43	0.52 6.26	-0.12 -2.27	0.27 2.77	-0.26 -2.20 ^b	0.57 3.19 ^b	0.58	0.44	-9.37 ^a	6.28 ^a	-2.36 ^c	34
44. Nigeria	0.63 5.27	-0.34 -2.75	0.59 2.50	0.55 3.49	0.17 3.49	0.95	0.67 7.21	-0.30 -3.10	0.60 3.25	-0.90 -6.96 ^a	1.81 7.59 ^a	1.81	0.94	-3.05	0.74	3.39 ^a	34
45. Norway	0.76 7.09	-0.41 -1.90	0.16 1.28	0.05 0.27	0.05 0.27	0.98	0.82 11.44	-0.39 -2.52	0.09 1.08	-2.22 -2.68 ^b	0.53 1.79 ^c	0.52	0.98	-5.01 ^a	-1.47	-1.58	34
46. Pakistan	0.04 0.26	-0.52 -4.40	0.83 5.27	0.27 1.58	0.11 1.58	0.85	0.15 1.17	-0.42 -4.71	0.70 5.95	-0.49 -6.35 ^a	0.82 11.22 ^a	0.83	0.84	-4.18 ^b	6.67 ^a	-2.40	34
47. Panama	0.49 2.60	-0.01 -0.03	0.46 2.34	0.40 2.31	0.11 2.31	0.93	0.62 4.28	-0.06 -0.43	0.38 2.54	-0.16 -0.40	0.99 9.73 ^a	1.00	0.91	-3.57	2.06	-0.06	34
48. Papua New Guinea	0.65 8.93	-0.27 -1.99	0.79 3.29	0.25 1.28	0.08 1.28	0.96	0.75 11.63	-0.27 -2.25	0.47 2.17	-1.08 -2.11 ^c	1.86 3.77 ^b	1.90	0.96	-9.44 ^a	-0.16	1.74	33
49. Paraguay	0.53 2.98	-0.16 -1.13	0.72 2.60	0.10 0.56	0.20 0.56	0.93	0.56 5.46	-0.14 -1.73	0.69 4.15	-0.33 -1.82 ^b	1.58 15.81 ^a	1.57	0.94	-4.56 ^b	3.76 ^a	5.78 ^a	34
50. Peru	0.53 4.63	-0.32 -3.04	0.19 2.15	0.39 2.29	0.11 2.29	0.65	0.67 5.80	-0.21 -2.05	0.17 1.93	-0.63 -1.75	0.50 2.13 ^c	0.52	0.62	-3.99 ^c	1.02	-2.09	34

51. Philippines	0.79 7.56	-0.36 -2.22	0.44 2.27	0.43 2.38	0.09 0.97	0.89 9.02	-0.29 -1.79	0.24 1.31	-2.73 -1.39	2.25 3.22 ^b	-2.73	2.26	0.09	0.97	-3.14	-0.88	1.79	34
52. Portugal	0.73 6.47	-0.38 -2.73	0.40 2.20	0.18 0.96	0.10 0.97	0.75 9.07	-0.29 -2.86	0.35 2.65	-1.18 -3.51 ^a	1.42 9.00	-1.14	1.42	0.07	0.97	-4.24 ^b	-0.53	2.67 ^b	34
53. Rwanda	0.38 2.34	-0.12 -0.67	0.98 3.63	-0.04 -0.24	0.14 0.96	0.49 4.61	-0.04 -0.33	0.83 4.85	-0.07 -0.34	1.63 18.72 ^a	-0.08	1.61	0.09	0.96	-6.51 ^a	4.31 ^a	7.21 ^a	34
54. South Africa	0.50 3.96	-0.53 -3.43	0.33 3.39	0.19 1.10	0.10 0.87	0.56 8.65	-0.44 -5.63	0.30 5.98	-1.00 -5.58 ^a	0.67 11.45 ^a	-1.04	0.68	0.05	0.87	-5.23 ^a	-0.02	-5.62 ^a	34
55. Spain	0.56 4.94	-0.35 -3.52	0.75 2.80	0.46 2.69	0.07 0.99	0.64 4.79	-0.26 -2.31	0.61 1.95	-0.74 -2.43 ^b	1.70 6.01 ^a	-0.74	1.71	0.08	0.99	-3.50	0.84	2.47 ^c	34
56. Sweden	0.57 5.26	-0.06 -0.77	0.94 3.57	0.00 -0.02	0.04 0.99	0.67 7.45	-0.05 -0.95	0.71 3.15	-0.16 -1.00	2.13 14.04 ^a	-0.16	2.18	0.03	0.99	-5.28 ^a	5.33 ^a	7.46 ^a	34
57. Switzerland	0.87 8.71	-0.22 -1.22	-0.05 -0.24	0.23 1.32	0.06 0.98	0.92 9.98	-0.13 -0.76	0.02 0.09	-1.64 -1.50	0.23 0.09	-1.73	0.23	0.05	0.98	-3.97 ^c	-0.58	-0.32	34
58. Thailand	0.69 5.30	-0.51 -2.66	0.55 2.69	0.46 2.87	0.11 0.98	0.74 7.65	-0.38 -2.52	0.44 2.86	-1.43 -2.74 ^b	1.67 10.29 ^a	-1.37	1.69	0.08	0.98	-3.62	-0.82	4.13 ^a	34
59. Trinidad and Tobago	0.50 5.00	-0.49 -5.15	0.25 2.52	0.16 0.85	0.12 0.98	0.57 6.91	-0.44 -5.43	0.22 2.51	-1.02 -15.51 ^a	0.50 3.16 ^b	-1.07	0.50	0.10	0.98	-4.88 ^a	-0.35	-3.12 ^b	34
60. Turkey	0.86 5.68	0.03 0.27	0.21 0.89	0.18 0.93	0.14 0.96	0.93 8.58	-0.03 -0.32	0.13 0.73	-0.35 -0.35	1.78 2.30 ^b	-0.34	1.80	0.10	0.95	-4.29 ^b	0.65	1.01	34
61. United Kingdom	0.49 6.61	-0.01 -0.16	1.23 6.72	0.09 0.50	0.03 1.00	0.56 9.08	-0.03 -0.71	1.08 7.01	-0.07 -0.70	2.43 30.34 ^a	-0.07	2.45	0.02	0.99	-5.26 ^a	9.77 ^a	17.8 ^a	34
62. United States	0.44 4.92	-0.25 -4.80	1.35 6.57	0.19 1.05	1.00	0.56 5.99	-0.23 -4.53	1.09 4.94	-0.52 -3.67 ^b	2.45 33.56 ^a	-0.50	2.51	0.04	1.00	-5.06 ^a	3.45 ^a	19.8 ^a	34

Table A1. (concluded)

	OLS estimates					FM estimates													
	m_{-1}	p	gdp_x	AC	ser	R^2	m_{-1}	p	gdp_x	E_p	E_y	E_p^c	E_y^c	ser	R^2	$P-O$	$E_p = -1$	$E_y = 1$	$nobs$
63. Uruguay	0.68	-0.20	1.38	0.22	0.12	0.92	0.77	-0.22	1.24	-0.99	5.48	-0.94	5.54	0.11	0.91	-3.78	0.02	3.23 ^b	34
	6.93	-1.93	3.94	1.30			8.24	-2.27	3.63	-1.66	3.95 ^a								
64. Yugoslavia	0.69	-0.41	0.35	0.25	0.09	0.94	0.80	-0.33	0.25	-1.67	1.24	-1.65	1.22	0.09	0.94	-3.85 ^c	-1.11	0.81	31
	6.91	-3.74	2.58	1.24			8.34	-3.16	1.93	-2.76 ^a	4.21 ^a								
65. Zaire	0.92	-0.02	0.11	-0.14	0.18	0.90	0.93	-0.02	0.00	-0.34	0.03	-0.35	0.03	0.10	0.90	-5.60 ^a	0.94	-0.29	30
	9.48	-0.26	0.33	-0.66			18.10	-0.43	0.01	-0.49	0.01								
66. Zambia	0.56	-0.51	0.16	0.06	0.11	0.93	0.62	-0.44	0.13	-1.17	0.34	-1.22	0.34	0.09	0.93	-8.82 ^a	-1.25	-4.86 ^a	34
	5.72	-4.56	2.28	0.32			8.35	-5.17	2.31	-8.55 ^a	2.45 ^c								
Mean	0.59	-0.32	0.56				0.68	-0.26	0.45	-1.08	1.45	-1.07	1.46						
Median	0.60	-0.31	0.48				0.69	-0.22	0.32	-0.80	1.32	-0.79	1.33						
Standard deviation	0.21	-0.21	0.39				0.19	0.19	0.34	1.08	0.93	1.06	0.93						
Minimum	-0.01	-0.94	-0.05				0.10	-0.86	0.00	-6.74	0.03	-6.66	0.03						
Maximum	1.00	0.03	1.72				0.96	-0.01	1.36	-0.02	5.48	-0.01	5.54						

Notes: The dependent variable is real imports of goods and nonfactor services (m). The explanatory variables are the lagged dependent variable (m_{-1}), the real exchange rate (p) computed as the ratio of imports deflator to GDP deflator, and GDP minus exports (gdp_x). The import demand equation is estimated using both OLS and the Phillips-Hansen FM estimator. The long-run price and income elasticities are given by E_p and E_y , respectively. E_p^c and E_y^c give the long-run price and income elasticities corrected for bias (see Table 4). For each country, the estimated coefficients and their t -statistic (below the coefficient estimates) are provided. The following statistics are provided: Durbin's test for autocorrelation (AC), R^2 , standard error of the regression (ser), and the number of observations for each country ($nobs$). Cointegration between the three variables in the import demand equation is tested using the Phillips-Ouliaris residual test given in column $P-O$. Finally, the columns labeled $E_p = -1$ and $E_y = 1$ report the two-tailed t -test for unit-price and unit-income elasticities, respectively. The asymptotic critical values for the Phillips-Ouliaris test at 10 percent, 5 percent, and 1 percent are, respectively, -3.84, -4.16, and -4.64. The superscripts a , b , and c indicate significance at 1 percent, 5 percent, and 10 percent respectively. Exact critical values (from Table 5) are used to compute the significance level of E_p , E_y , E_p^c , $E_y^c = -1$, and $E_y = 1$.

REFERENCES

- Andrews, Donald W.K., and J. Christopher Monahan, 1991, "An Improved Heteroskedasticity and Autocorrelation Consistent Matrix Estimator," *Econometrica*, Vol. 60, pp. 953-66.
- Buse, A., 1973, "Goodness of Fit in Generalized Least Squares Estimation," *The American Statistician*, Vol. 27, pp. 106-108.
- Clarida, Richard H., 1994, "Co-integration, Aggregate Consumption, and the Demand for Imports: A Structural Econometric Investigation," *American Economic Review*, Vol. 84 (March), pp. 298-308.
- Faini, R., L. Pritchett, and F. Clavijo, 1992, "Import Demand in Developing Countries," in *International Trade Modelling*, ed. by M.G. Dagenais and P.A. Muet (New York: Chapman and Hall), pp. 279-97.
- Feenstra, Robert C., 1994, "New Product Varieties and the Measurement of International Prices," *American Economic Review*, Vol. 84 (March), pp. 157-77.
- Goldstein, Morris, and Mohsin Khan, 1985, "Income and Price Effect in Foreign Trade," in *Handbook of International Economics*, ed. by Ronald W. Jones and Peter B. Kenen (Amsterdam: North-Holland), pp. 1042-99.
- Hansen, B.E., 1992, "Efficient Estimation and Testing of Cointegrating Vectors in the Presence of Deterministic Trends," *Journal of Econometrics*, Vol. 53 (July-September), pp. 87-121.
- Houthakker, Hendrik S., 1960, "Additive Preferences," *Econometrica*, Vol. 28, pp. 244-57.
- Marston, Richard, 1990, "Pricing to Market in Japanese Manufacturing," *Journal of International Economics*, Vol. 29 (November), pp. 217-36.
- Ogaki, Masao, 1992, "Engel's Law and Cointegration," *Journal of Political Economy*, Vol. 100 (October), pp. 1027-46.
- Pesaran, H., and Shin, Y. 1998, "An Autoregressive Distributed Lag Modelling Approach to Cointegration Analysis," forthcoming in *Centennial Volume of Ragnar Frisch*, ed. by S. Strom, A. Holly, and P. Diamon (Cambridge: Cambridge University Press).
- Phillips, P.C.B., and B.E. Hansen, 1990, "Statistical Inference in Instrumental Variables Regression with I(1) Processes," *Review of Economic Studies*, Vol. 57, pp. 99-125.
- Phillips, Peter C.B., and Mico Loretan, 1991, "Estimating Long-run Economic Equilibria," *Review of Economic Studies*, Vol. 58 (May), pp. 407-36.
- Reinhart, Carmen M., 1995, "Devaluation, Relative Prices, and International Trade," *Staff Papers*, International Monetary Fund, Vol. 42 (June), pp. 290-312.
- Stock, James H., and Mark W. Watson, 1988, "Testing for Common Trends," *Journal of the American Statistical Association*, Vol. 83 (December), pp. 1097-1107.

Swagel, Phillip, 1995, "Import Prices and the Competing Goods Effect," International Finance Discussion Paper No. 508 (Washington: Board of Governors of the Federal Reserve System, April).

Thursby, Jerry, and Marie Thursby, 1984, "How Reliable Are Simple, Single Equation Specifications of Import Demand?" *Review of Economics and Statistics*, Vol. 66 (February), pp. 120-28.